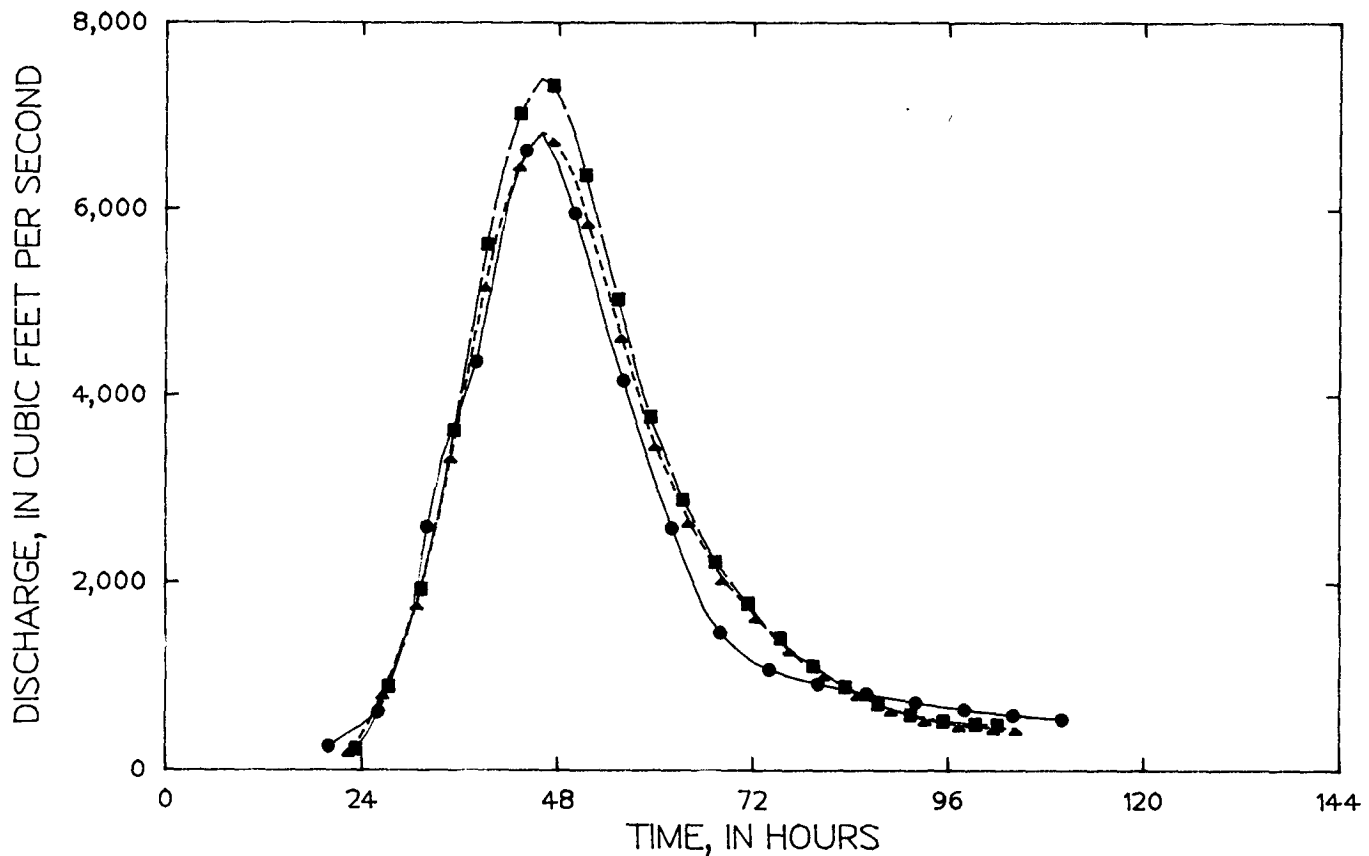


TECHNIQUES FOR SIMULATING FLOOD HYDROGRAPHS AND ESTIMATING FLOOD VOLUMES FOR UNGAGED BASINS IN EAST AND WEST TENNESSEE



Prepared by the
U.S. GEOLOGICAL SURVEY

in cooperation with the
TENNESSEE DEPARTMENT OF TRANSPORTATION



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By Charles R. Gamble

U.S. GEOLOGICAL SURVEY

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CONVERSION FACTORS

For readers who may prefer to use metric units rather than the inch-pound units used herein, the conversion factors are listed below:

| Multiply inch-pound unit | By | To obtain metric unit |
|--|-----------|--|
| inch (in.) | 2.54 | centimeter (cm) |
| foot (ft) | 0.3048 | meter (m) |
| mile (mi) | 1.609 | kilometer (km) |
| square mile (mi ²) | 2.590 | square kilometer (km ²) |
| cubic foot per second (ft ³ /s) | 0.02832 | cubic meter per second (m ³ /s) |

TECHNIQUES FOR SIMULATING FLOOD HYDROGRAPHS AND ESTIMATING FLOOD VOLUMES FOR UNGAGED BASINS IN EAST AND WEST TENNESSEE

By Charles R. Gamble

ABSTRACT

A dimensionless hydrograph developed for a variety of basin conditions in Georgia was tested for its applicability to streams in East and West Tennessee by comparing it to a similar dimensionless hydrograph developed for streams in East and West Tennessee. Eighty-three observed hydrographs in East Tennessee and 38 in West Tennessee were used in the study. Statistical analyses were performed by comparing simulated (or computed) hydrographs, derived by application of the Georgia dimensionless hydrograph, and dimensionless hydrographs developed from Tennessee data, with the observed hydrographs at 50 and 75 percent of their peak flow widths. Results of the tests indicate that the Georgia dimensionless hydrograph is virtually the same as the one developed for streams in East Tennessee but that it is different from the dimensionless hydrograph developed for streams in West Tennessee. Because of the extensive testing of the Georgia dimensionless hydrograph, it was determined to be applicable for East Tennessee, whereas the dimensionless hydrograph developed from data on West Tennessee streams was determined to be applicable for West Tennessee.

As part of the dimensionless hydrograph development, an average lagtime in hours, for each study basin, and the volume in inches, of flood runoff for each flood event were computed. By use of multiple-regression analyses, equations were developed that relate basin lagtime to drainage area size, basin length, and percent impervious area.

Similarly, flood volumes were related to drainage area size, peak discharge, and basin lagtime. These equations, along with the appropriate dimensionless hydrograph, can be used to estimate a typical (average) flood hydrograph and volume for recurrence-intervals up to 100 years at any ungaged site draining less than 500 square miles in East or West Tennessee.

INTRODUCTION

Flood hydrographs and flood volumes commonly are needed for the design of highway drainage structures and embankments or where storage of floodwater or flood prevention is part of the design. Additionally, hydrographs may be necessary to estimate the length of time of inundation of specific features, for example, roads and bridges.

In design work, many times a hydrograph is needed for a site where no streamflow records are available. Under these conditions, a typical or design hydrograph may be simulated using one, or a combination of several, traditional hydrograph estimation methods. Each of the traditional methods has inherent characteristics, data requirements, and basin characteristics or coefficients that must be estimated or calculated. Most methods rely on the unit hydrograph, whereby design hydrographs are computed by convolution of the unit hydrograph with rainfall excess. Therefore, rainfall data and methods for

estimating rainfall excess are necessary for use of the unit hydrograph methods.

A need exists for a simple, direct-approach method to estimate the flood hydrograph, volume and width associated with a peak discharge of specific recurrence interval (a design discharge). Recently, a direct-approach method was developed for streams in Georgia (Inman, 1986). The applicability of this direct-approach method for Georgia streams has and is being tested in several areas of the United States, especially in the southeast. One such test, for central Tennessee, successfully demonstrated that the Georgia dimensionless hydrograph method works for streams in central Tennessee (Robbins, 1986).

This report describes the results of a study to determine the applicability of Inman's method to streams in East and West Tennessee. Techniques for estimating flood hydrographs (shape, volume, and width) for ungaged basins draining areas less than 500 mi² in these areas of Tennessee are provided. This study was conducted in cooperation with the Tennessee Department of Transportation.

INMAN'S HYDROGRAPH SIMULATION METHOD

Inman (1986) used 355 actual (observed) streamflow hydrographs from 80 basins, and harmonic analysis as described by O'Donnell (1960), to develop unit hydrographs. The 80 basins represented both urban and rural streamflow characteristics and had drainage areas less than 20 mi². An average unit hydrograph and an average lagtime were computed for each basin. These average unit hydrographs were then transformed to unit hydrographs having generalized durations of one-fourth, one-third, one-half, and three-fourths lagtime, then reduced to dimensionless terms by dividing the time by lagtime and the discharge by peak discharge. Representative dimensionless hydrographs developed

for each basin were combined to generate one typical (average) dimensionless hydrograph for each of the four generalized durations. Using the four generalized duration dimensionless hydrographs, average basin lagtime, and peak discharge for each observed hydrograph, simulated hydrographs were generated for each of the 355 observed hydrographs, and their widths were compared with the widths of the observed hydrographs at 50 and 75 percent of peak flow. Inman (1986) concluded that the dimensionless hydrographs based on the one-half lagtime duration provided the best fit of the observed data. At the 50 percent of peak-flow width, the standard error of estimate was 31.8 percent; and at the 75 percent of peak-flow width, the standard error of estimate was 35.9 percent.

For verification, the one-half lagtime duration dimensionless hydrograph was applied to 138 hydrographs from 37 Georgia stations that were not used in its development. The drainage areas of these stations ranged from 20 to 500 mi². Inman (1986) reported that at 50 percent of peak flow, the standard error of estimate of the width was 39.5 percent and at 75 percent of peak flow, the standard error of estimate of the width was 43.6 percent.

Inman (1986) performed a second verification to assess the total or cumulative prediction error for large floods through the combined use of the dimensionless hydrograph, estimated lagtimes from regional lagtime equations, and peak discharges from regional flood-frequency equations. Inman (1986) reported standard errors of prediction of 51.7 and 57.1 percent of peak flow widths, respectively, at 50 percent and 75 percent of peak flow.

On the basis that Inman's basic dimensionless hydrograph was developed and tested for a variety of conditions (including urban, rural, mountainous, coastal plain, and small and large drainage basins), and had been shown by Robbins (1986) to be applicable to central

Tennessee, it was theorized that it may be applicable to streams in East and West Tennessee.

TESTING INMAN'S DIMENSIONLESS HYDROGRAPH ON EAST AND WEST TENNESSEE STREAMS

Inman's dimensionless hydrograph was tested by comparing it to a similar dimensionless hydrograph developed for East Tennessee streams. The test involved several phases and is described in detail in this section of the report. The dimensionless hydrograph developed for West Tennessee was quite different from Inman's and, therefore, was not tested against it. However, it was tested to see how well it reproduced observed storms as described in this section of the report.

A total of 235 hydrographs of observed streamflow from 21 basins in East Tennessee having drainage areas ranging from 18.8 to 518 mi² and 119 hydrographs of observed streamflow from 10 basins having drainage areas ranging from 55.5 to 503 mi² in West Tennessee were available for use in the test (fig.1). However, only 83 observed hydrographs in East Tennessee and 38 in West Tennessee had concurrent rainfall data and were selected for use. The basins in East and West Tennessee were located within hydrologic areas 1 and 4, respectively, as defined by Randolph and Gamble (1976). A computer program package developed by S.E. Ryan, U.S. Geological Survey, Georgia District, was used for development of the dimensionless hydrographs and subsequent statistical analyses for this report.

Unit hydrographs and lagtime were computed from each of the observed hydrographs and matching rainfall, and an average lagtime was computed for each basin. In East Tennessee, six basins representing the size range and areal distribution were selected for computing an average unit hydrograph. In West Tennessee, all

10 basins were used to compute an average unit hydrograph. These average unit hydrographs for each area were transformed to unit hydrographs having generalized durations of one-fourth, one-third, one-half, and three-fourths lagtime, then reduced to dimensionless terms by dividing the time ordinates by lagtime and the discharge ordinates by peak discharge.

For both East and West Tennessee a CHECK procedure was used to test how well the computed dimensionless hydrograph could reproduce observed hydrographs, which was carried out as follows: The four generalized duration dimensionless hydrographs, average basin lagtimes, and peak discharges from the observed hydrographs were used to generate simulated hydrographs for the corresponding observed hydrographs. The simulated hydrograph widths were compared with the widths of the observed hydrographs at 50 and 75 percent of peak flow (table 1). Inman's dimensionless hydrograph (one-half lagtime duration), average basin lagtimes, and peak discharges from the observed hydrographs in East Tennessee were used to generate simulated hydrographs for the corresponding observed hydrographs. These hydrograph widths were also compared at the 50 and 75 percent of peak flow (table 1).

On the basis of the above tests, Inman's one-half lagtime duration dimensionless hydrograph is just as applicable to East Tennessee streams as the lagtime duration dimensionless hydrographs developed from data in that area. Standard errors of width comparison are essentially the same for the one-half-lagtime duration. Robbins (1986) found the same to be true for central Tennessee streams. Therefore, because of its extensive testing not only on Georgia streams but on streams in other parts of the southeast, including central Tennessee, Inman's dimensionless hydrograph is the preferred one to use for simulating hydrographs for streams in East Tennessee. Inman's one-half-lagtime duration dimensionless hydrograph is compared to the one-half-lagtime duration dimensionless

Table 1.--Results of CHECK procedure using dimensionless hydrographs developed from data as indicated

| East Tennessee | | | West Tennessee | | |
|---|---|-------------------------|------------------|---|-------------------------|
| Lagtime duration | Standard error, in percent, of width comparison | | Lagtime duration | Standard error, in percent, of width comparison | |
| | 50 percent of peak flow | 75 percent of peak flow | | 50 percent of peak flow | 75 percent of peak flow |
| 1/4 | 44.4 | 48.0 | 1/4 | 36.0 | 44.7 |
| 1/3 | 42.3 | 44.2 | 1/3 | 35.4 | 42.8 |
| 1/2 | 35.4 | 36.0 | 1/2 | 34.5 | 41.1 |
| 3/4 | 32.6 | 35.7 | 3/4 | 34.1 | 41.9 |
| Inman's dimensionless hydrograph (Applied to East Tennessee streams) | | | | | |
| | 1/2 | 35.2 | 35.1 | | |

hydrograph developed from data from East Tennessee streams in figure 2. The time and discharge ratios of Inman's dimensionless hydrograph are shown in table 2.

As mentioned earlier, the dimensionless hydrographs developed for West Tennessee basins were quite different (wider) from Inman's. From the CHECK test shown in table 1 and another test described in the next section of this report, it appears that the three-fourths lagtime duration dimensionless hydrograph is best for West Tennessee basins (fig. 3). Its time and discharge ratios are shown in table 3.

Verification of Dimensionless Hydrographs

A computer test procedure called VERIFY was performed to assess the total or cumulative prediction error for large floods through the combined use of the dimensionless hydrographs, estimated basin lagtimes from regression equations (as described in a later sec-

tion of this report), and discharges derived from regional flood-frequency equations. Randolph and Gamble (1976) provide a technique for estimating the peak discharge of a selected recurrence interval for rural streams in Tennessee, and Robbins (1984) provides a technique for estimating the peak discharge of a selected recurrence interval for urban basins draining areas less than 25 mi² in Tennessee. Neely (1984) developed methods for estimating peak discharge, storm runoff, and unit hydrographs for urban basins in Memphis and Shelby County.

This verification test used the observed hydrograph having the highest peak discharge and a station flood-frequency curve for each station. The test was conducted as follows. The recurrence interval of each observed peak discharge was determined from its station-frequency curve. The appropriate regional regression flood-frequency equation, from Randolph and Gamble (1976), was then used to estimate the corresponding peak discharge for this recurrence interval. For each station, a basin lagtime was estimated from the appropriate regional basin lagtime equation (presented in a

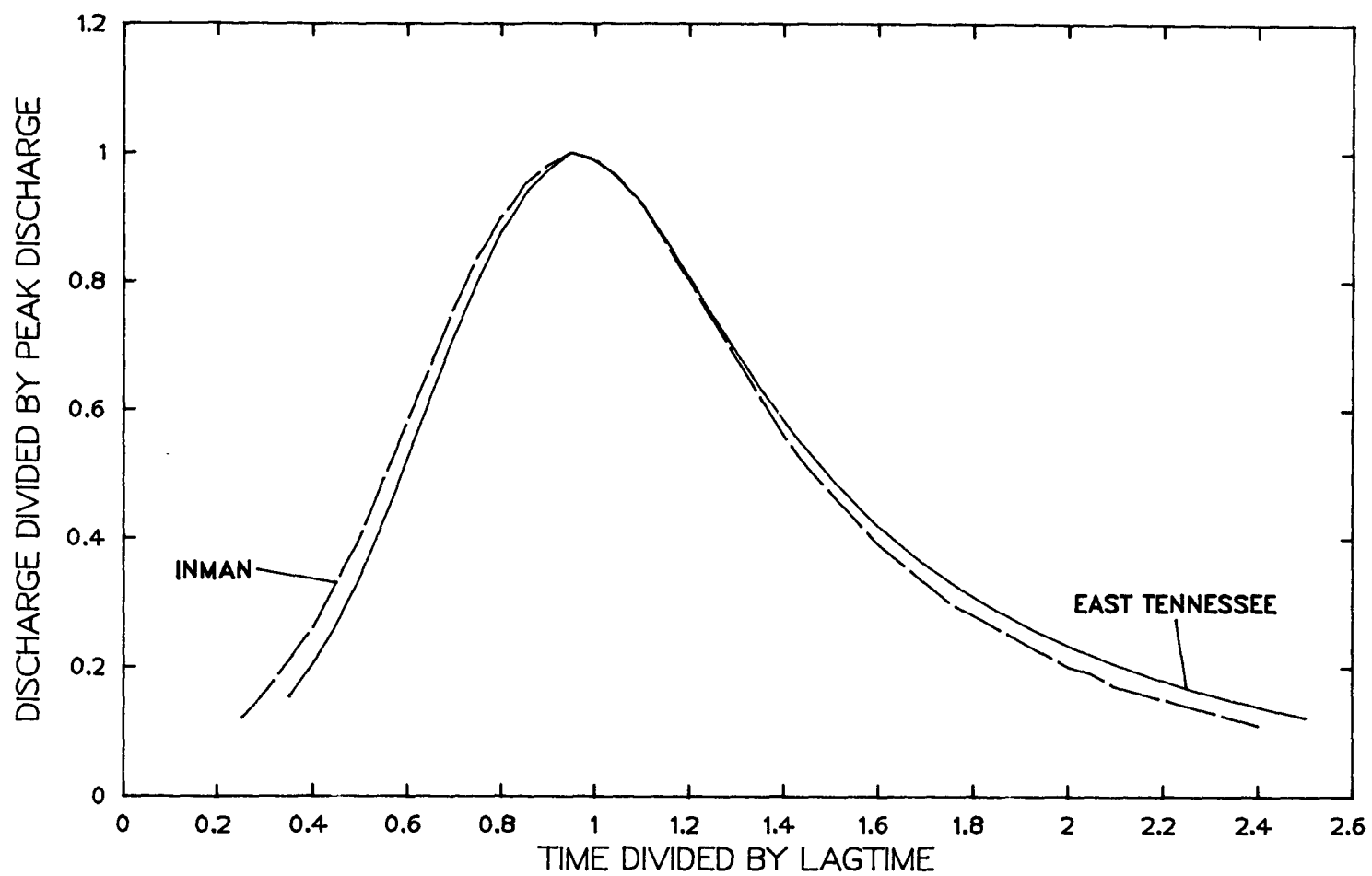


Figure 2. — Inman's and East Tennessee dimensionless hydrographs.

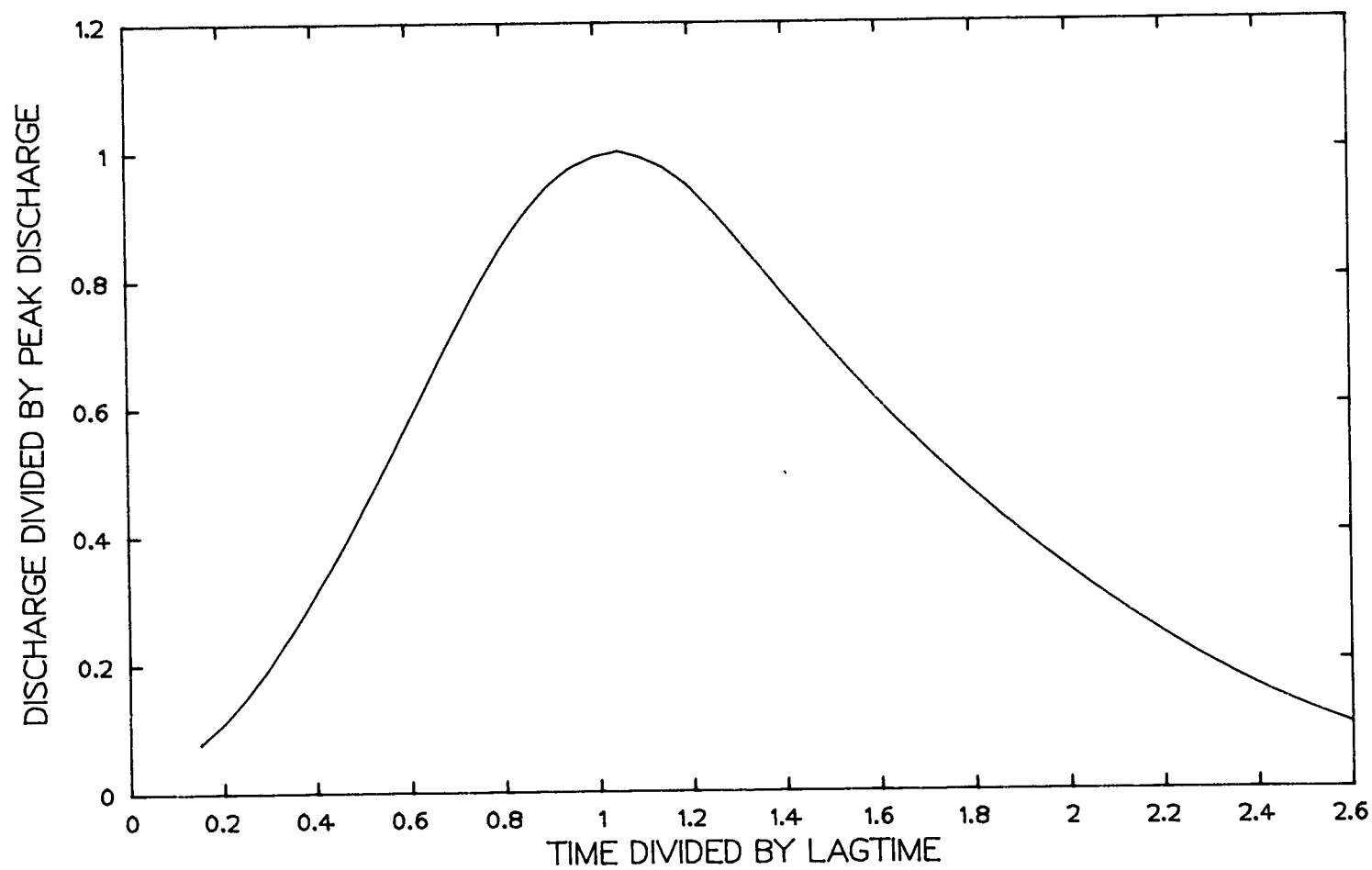


Figure 3. – Dimensionless hydrograph for West Tennessee.

Table 2.--Time and discharge ratios of Inman's dimensionless hydrograph

| Time ratio (t/LT) | Discharge ratio (Q _t /Q _p) | Time ratio (t/LT) | Discharge ratio (Q _t /Q _p) |
|----------------------|--|----------------------|--|
| 0.25 | 0.12 | 1.35 | 0.62 |
| .30 | .16 | 1.40 | .56 |
| .35 | .21 | 1.45 | .51 |
| .40 | .26 | 1.50 | .47 |
| .45 | .33 | 1.55 | .43 |
| .50 | .40 | 1.60 | .39 |
| .55 | .49 | 1.65 | .36 |
| .60 | .58 | 1.70 | .33 |
| .65 | .67 | 1.75 | .30 |
| .70 | .76 | 1.80 | .28 |
| .75 | .84 | 1.85 | .26 |
| .80 | .90 | 1.90 | .24 |
| .85 | .95 | 1.95 | .22 |
| .90 | .98 | 2.00 | .20 |
| .95 | 1.00 | 2.05 | .19 |
| 1.00 | .99 | 2.10 | .17 |
| 1.05 | .96 | 2.15 | .16 |
| 1.10 | .92 | 2.20 | .15 |
| 1.15 | .86 | 2.25 | .14 |
| 1.20 | .80 | 2.30 | .13 |
| 1.25 | .74 | 2.35 | .12 |
| 1.30 | .68 | 2.40 | .11 |

later section of this report). The estimated peak discharge, the estimated basin lagtime for each basin, and the appropriate dimensionless hydrograph (Inman's for East Tennessee and the one developed in this report for West Tennessee) were then used to generate simulated flood hydrographs. A comparison of the simulated and observed hydrograph widths at 50 and 75 percent of peak flow was made (table 4).

The range in recurrence intervals of the floods used in this test for East Tennessee streams was from 5 to greater than 100 years; the range for West Tennessee streams was from 3 to 43 years. These recurrence intervals are based on station frequency curves computed by methods recommended by the U.S. Water Resources Council (1981) using data through 1986.

Example comparisons between observed hydrographs and simulated hydrographs based

on observed peak discharge and measured basin lagtime and regression discharge and regression basin lagtime are shown in figures 4-7. The comparisons show fairly good agreement between the observed and simulated hydrographs. Peak discharges of the simulated hydrograph based on regression (estimated) discharge and regression (estimated) lagtime may not coincide with the observed peak discharges because the simulated hydrographs incorporate the error inherent in the regional flood-frequency relations and the regional lagtime equations. In some cases, differences in peak discharges may be quite large. Regression peak discharges are sometimes less than 50 percent of the observed-storm peak discharge. In this case, the difference in widths of the simulated and observed hydrographs at 50 and 75 percent of peak flow is 100 percent. This is why the standard errors of this comparison are somewhat high (table 4). These errors are representative of the total error that might occur at an ungaged site.

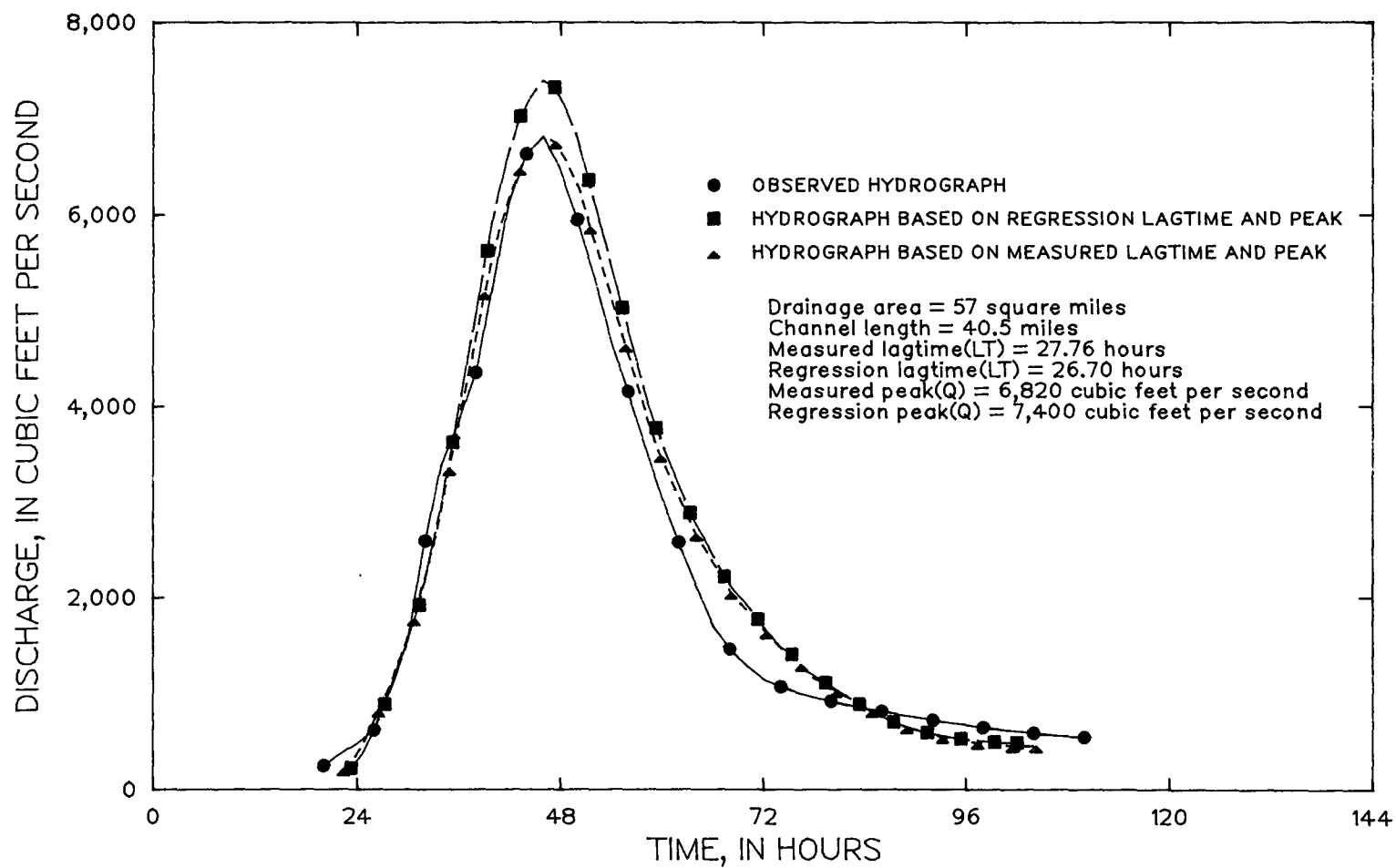


Figure 4. — Observed and simulated hydrographs for Oostanaula Creek near Sanford, Tenn. (03565500), for storm of March 12, 1963.

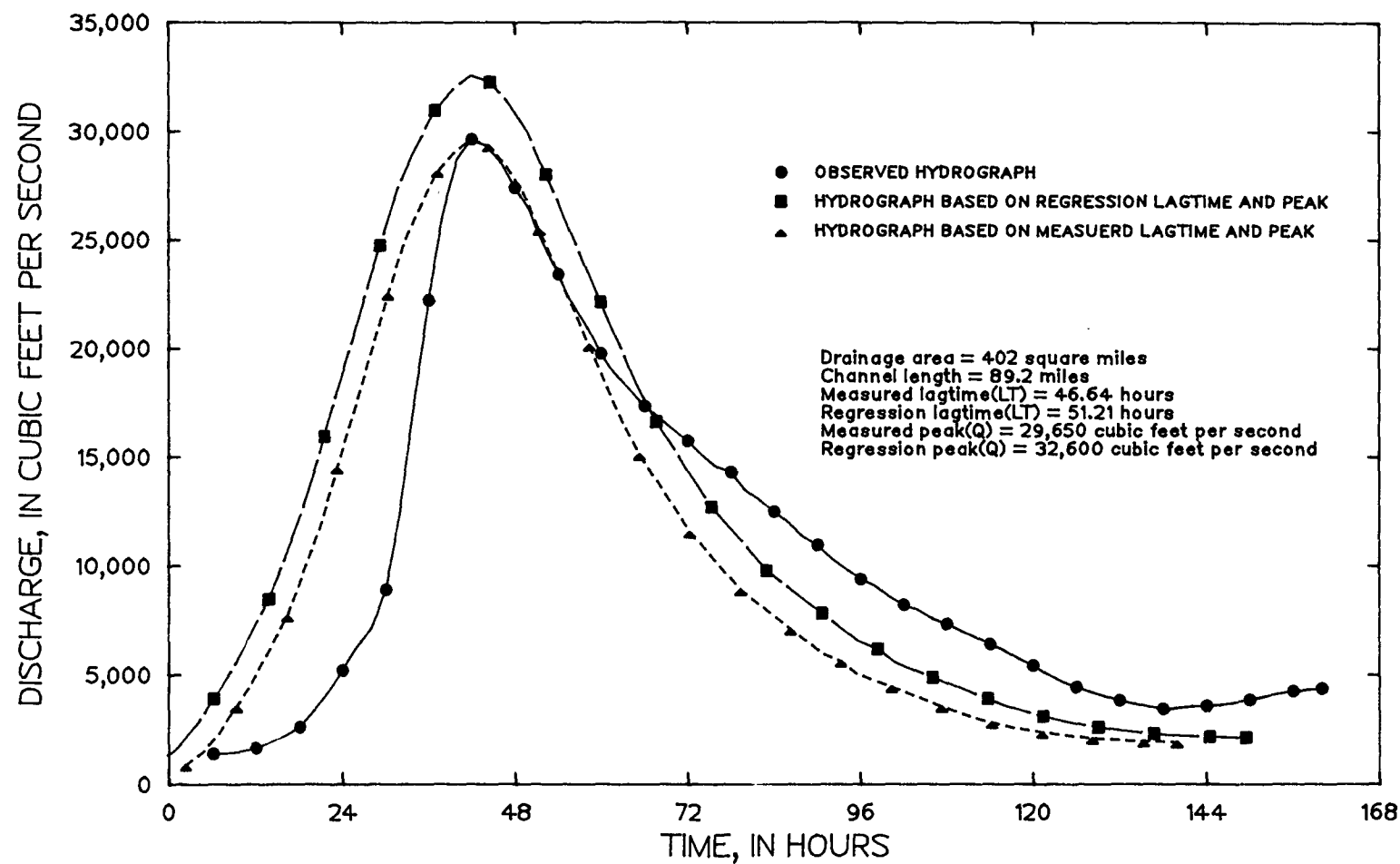


Figure 5. – Observed and simulated hydrographs for Sequatchie River near Whitwell, Tenn. (03571000), for storm of March 16, 1973.

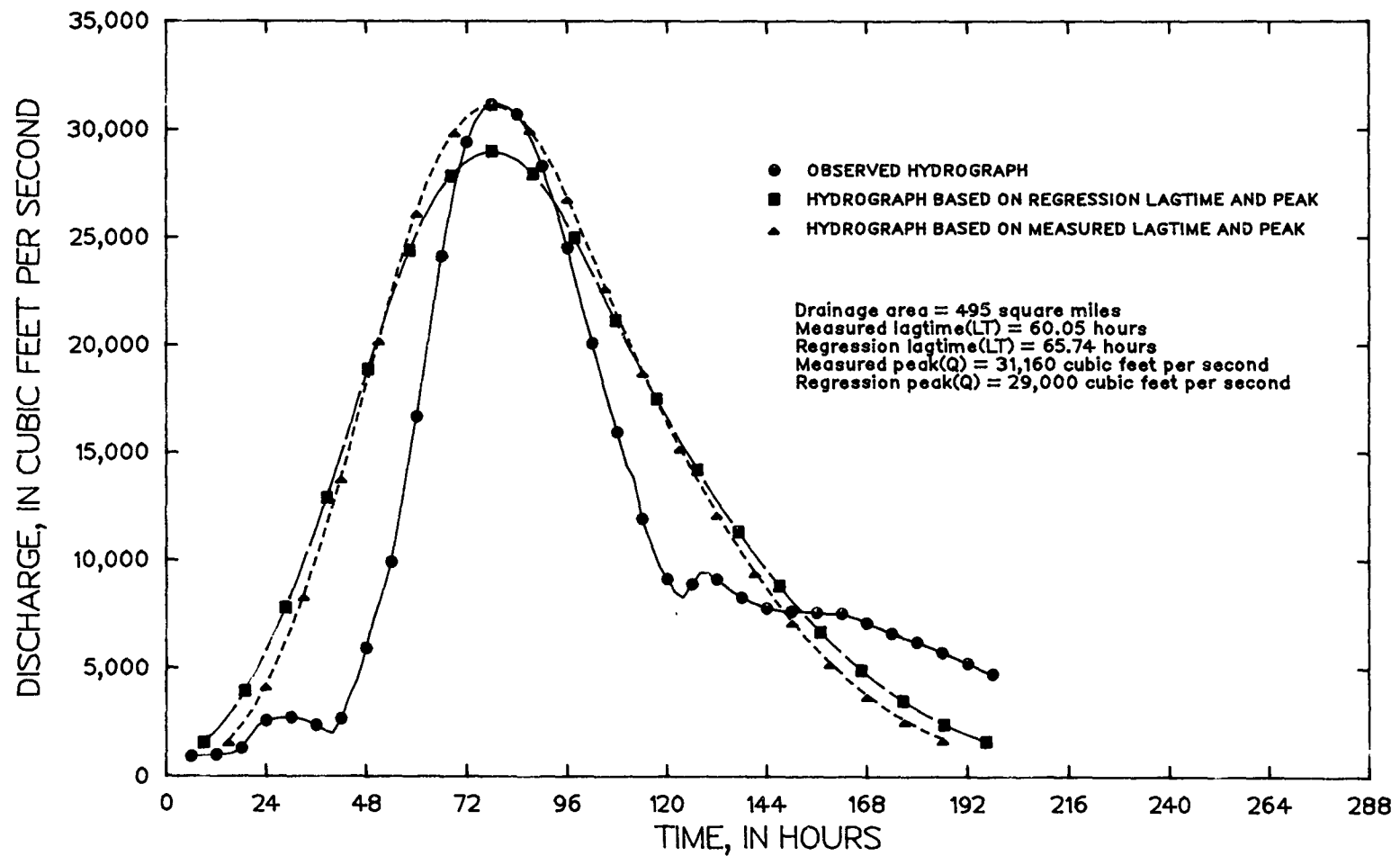


Figure 6. – Observed and simulated hydrographs for South Fork Forked Deer River at Jackson, Tenn. (07027500), for storm of April 21, 1973.

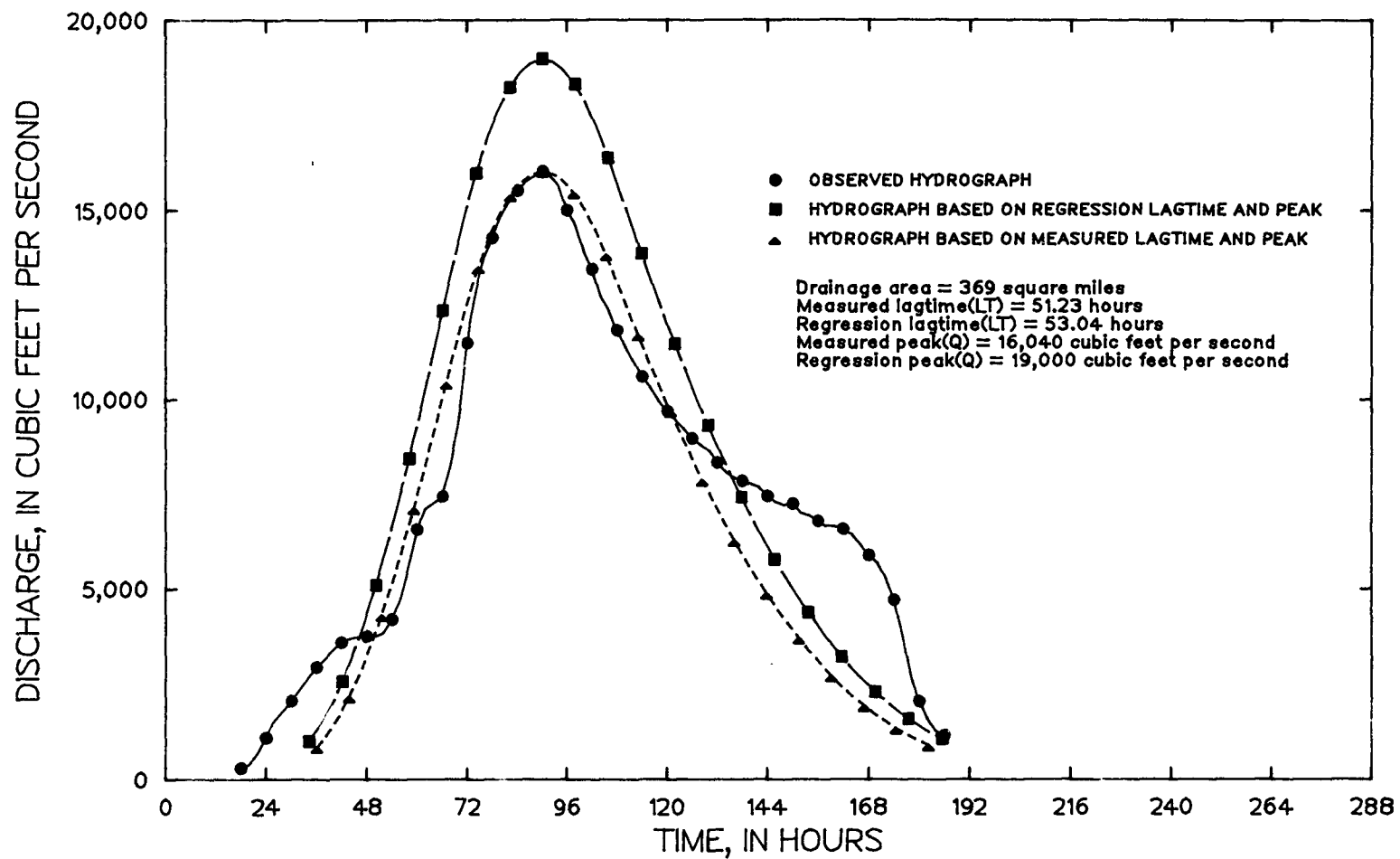


Figure 7. — Observed and simulated hydrographs for Middle Fork Forked Deer River near Alamo, Tenn. (07029000), for storm of February 12, 1965.

Table 3.--Time and discharge ratios of the West Tennessee dimensionless hydrograph

| Time ratio (t/LT) | Discharge ratio (Q _t /Q _p) | Time ratio (t/LT) | Discharge ratio (Q _t /Q _p) |
|----------------------|--|----------------------|--|
| 0.15 | 0.05 | 1.60 | 0.77 |
| .20 | .07 | 1.65 | .73 |
| .25 | .10 | 1.70 | .69 |
| .30 | .14 | 1.75 | .64 |
| .35 | .17 | 1.80 | .60 |
| .40 | .22 | 1.85 | .56 |
| .45 | .27 | 1.90 | .53 |
| .50 | .32 | 1.95 | .49 |
| .55 | .38 | 2.00 | .46 |
| .60 | .44 | 2.05 | .42 |
| .65 | .51 | 2.10 | .39 |
| .70 | .58 | 2.15 | .36 |
| .75 | .65 | 2.20 | .33 |
| .80 | .72 | 2.25 | .30 |
| .85 | .78 | 2.30 | .28 |
| .90 | .84 | 2.35 | .25 |
| .95 | .89 | 2.40 | .23 |
| 1.00 | .93 | 2.45 | .21 |
| 1.05 | .96 | 2.50 | .19 |
| 1.10 | .98 | 2.55 | .17 |
| 1.15 | .99 | 2.60 | .15 |
| 1.20 | 1.00 | 2.65 | .14 |
| 1.25 | .99 | 2.70 | .12 |
| 1.30 | .98 | 2.75 | .11 |
| 1.35 | .96 | 2.80 | .09 |
| 1.40 | .94 | 2.85 | .08 |
| 1.45 | .90 | 2.90 | .07 |
| 1.50 | .86 | 2.95 | .06 |
| 1.55 | .82 | 3.00 | .06 |

Table 4.--Results of the VERIFY procedure for East and West Tennessee

| East Tennessee | | | West Tennessee | | |
|-------------------------------------|---------------------------------------|----------------------------|---------------------|---------------------------------------|----------------------------|
| Lagtime duration | Standard error of width comparison | | Lagtime duration | Standard error of width comparison | |
| | 50 percent of peak flow | 75 percent of peak flow | | 50 percent of peak flow | 75 percent of peak flow |
| 1/4 | 73.3 | 85.4 | 1/4 | 59.2 | 74.5 |
| 1/3 | 68.8 | 80.2 | 1/3 | 48.3 | 46.5 |
| 1/2 | 54.1 | 67.9 | 1/2 | 51.6 | 53.5 |
| 3/4 | 46.6 | 65.2 | 3/4 | 48.8 | 46.9 |
| Inman's dimensionless hydrograph | | | | | |
| | 1/2 | 56.5 | | 70.4 | |

REGIONALIZATION OF BASIN LAGTIME AND FLOOD VOLUME

Estimating Basin Lagtime

Average basin lagtime is used as the principal time factor in the dimensionless hydrograph. Lagtime is generally considered to be constant for a basin (as long as basin conditions remain the same) and is defined as the elapsed time from the centroid of rainfall excess to the centroid of the resultant runoff hydrograph (Stricker and Sauer, 1982). The lagtime of a basin is the principal factor in determining the relative shape of a hydrograph from that basin. For example, a long lagtime will produce a broad flat-crested hydrograph and a short lagtime will produce a narrow sharp-crested hydrograph. Since lagtime is usually not known for a basin, it is often estimated from basin characteristics.

To provide a method of estimating lagtime for ungaged basins in East and West Tennessee, average basin lagtimes obtained from the dimensionless hydrograph development procedure and measured lagtime from rainfall-runoff modeling studies by Wibben (1976) and Robbins (1984) were related to their basin characteristics. Rural and urban basins were analyzed separately because of the effects of urbanization on lagtime. The paucity of lagtime data for urban streams in East Tennessee prevented the development of a lagtime equation for urban streams in that area. Neely (1984) developed a regression equation for computing the lagtime of urban basins in Shelby County which has a lower standard error of estimate than the lagtime equation for all of West Tennessee given herein. Therefore, it is recommended that Neely's equation be used for computing lagtime of urban basins in Shelby County (see "Supplemental Information"). Standard multiple linear regression techniques were used to develop equations for estimating rural and urban basin lagtimes from five basin characteristics. All five characteristics defined below were used in the regression analyses; how-

ever, only those characteristics statistically significant at the 95-percent confidence level are included in the final equations. Definitions of these basin characteristics are as follows:

Drainage area (DA) the contributing drainage area of the basin, in square miles.

Channel slope (CS) is the slope, in feet per mile, of the main channel determined from the difference in elevation at 10 and 85 percent of the distance along the main channel from the discharge site to the drainage-basin divide.

Channel length (CL) is the distance, in miles, from the discharge site to the drainage-basin divide, measured along the main water course.

CL/\sqrt{CS} is a ratio, where CL and CS are as previously defined.

Percentage of impervious area (IA) is the percentage of the contributing drainage area that is impervious to infiltration of rainfall. This parameter was measured using the grid method on recent aerial photographs. IA can also be measured from topographic maps or from population and industrial density reports.

All of the basins and their characteristics used in the regression analyses are listed in table 5.

Regression Analyses

Stepwise regression techniques were used with the five basin characteristics to derive equations for estimating basin lagtime (table 6). Only the characteristics shown in each equation were statistically significant at the 95-percent confidence level for that locality and category of stream. The distribution of the drainage area size

Table 5.--Stations and drainage basin characteristics used in lagtime regression analyses

[Stations with a value for percentage of impervious area are on streams draining urban areas and were used in the urban lagtime regression analysis; mi², square miles; mi, mile; ft/mi, foot per mile; h, hour]

| Station No. | Name | Drainage area, DA (mi ²) | Percentage of impervious area IA, (percent) | Channel length, CL (mi) | Channel slope CS (ft/mi) | Average basin lagtime, LT (h) | Estimated lagtime from equations, LT (h) |
|-----------------------|--|--------------------------------------|---|-------------------------|--------------------------|-------------------------------|--|
| <u>East Tennessee</u> | | | | | | | |
| 03418900 | Raccoon Creek near Old Winesap, Tenn. | 1.52 | - | 1.88 | 182.27 | 3.58 | 2.12 |
| 03461200 | Cosby Creek above Cosby, Tenn. | 10.2 | - | 4.40 | 484.85 | 3.88 | 4.28 |
| 03467000 | Lick Creek at Mohawk, Tenn. | 220 | - | 50.4 | 4.21 | 29.42 | 31.98 |
| 03469110 | Ramsey Creek near Pittman Center, Tenn. | 2.18 | - | 3.05 | 649.44 | 6.55 | 3.16 |
| 03470000 | Little Pigeon River at Sevierville, Tenn. | 353 | - | 32.1 | 76.3 | 14.84 | 22.04 |
| 03485500 | Doe River at Elizabethton, Tenn. | 137 | - | 28.4 | 58.9 | 16.61 | 19.92 |
| 03486225 | Powder Branch near Johnson City, Tenn. | 4.88 | - | 3.87 | 124.83 | 1.13 | 3.85 |
| 03491000 | Big Creek near Rogersville, Tenn. | 47.3 | - | 20.1 | 14.4 | 12.27 | 14.98 |
| 03497300 | Little River above Townsend, Tenn. | 106 | - | 23.85 | 101.5 | 19.04 | 17.25 |
| 03498500 | Little River near Maryville, Tenn. | 269 | - | 42.7 | 53.6 | 19.14 | 27.89 |
| 03518500 | Tellico River at Tellico Plains, Tenn. | 118 | - | 27.8 | 90.5 | 14.18 | 19.58 |
| 03519610 | Baker Creek tributary near Binfield, Tenn. | 2.10 | - | 2.22 | 63.36 | 1.65 | 2.43 |
| 03519630 | Griffitts Branch near Greenback, Tenn. | 1.46 | - | 1.19 | 100.32 | 1.41 | 1.45 |
| 03519640 | Baker Creek near Greenback, Tenn. | 16.0 | - | 8.79 | 17.42 | 6.71 | 7.57 |
| 03519650 | Little Baker Creek near Greenback, Tenn. | 3.65 | - | 4.07 | 29.57 | 2.25 | 4.01 |
| 03535000 | Bullrun Creek near Halls Crossroads, Tenn. | 68.5 | - | 26.4 | 15.2 | 19.26 | 18.76 |
| 03535140 | South Fork Beaver Creek at Harbison, Tenn. | 1.23 | - | 1.72 | 52.80 | 1.54 | 1.97 |
| 03535160 | Beaver Creek near Halls Crossroads, Tenn. | 14.1 | - | 6.78 | 15.84 | 5.03 | 6.11 |
| 03535180 | Willow Fork near Halls Crossroads, Tenn. | 3.23 | - | 4.58 | 58.08 | 3.08 | 4.42 |
| 03538225 | Poplar Creek near Oak Ridge, Tenn. | 82.5 | - | 20.2 | 13.22 | 24.05 | 15.04 |
| 03538250 | East Fork Poplar Creek near Oak Ridge, Tenn. | 19.5 | - | 12.65 | 12.87 | 11.71 | 10.22 |
| 03538900 | Self Creek near Big Lick, Tenn. | 3.80 | - | 3.67 | 45.41 | 6.25 | 3.68 |
| 03539100 | Byrd Creek near Crossville, Tenn. | 1.10 | - | 1.66 | 40.13 | 3.12 | 1.91 |
| 03539600 | Daddys Creek near Hebbertsburg, Tenn. | 139 | - | 39.6 | 8.65 | 21.58 | 26.21 |
| 03539800 | Obed River near Lancing, Tenn. | 518 | - | 56.3 | 17.2 | 24.72 | 35.04 |
| 03541100 | Bitter Creek near Camp Austin, Tenn. | 5.53 | - | 4.05 | 190.08 | 1.89 | 4.00 |
| 03541200 | Forked Creek near Oakdale, Tenn. | 2.44 | - | 3.03 | 237.60 | 2.58 | 3.14 |
| 03543500 | Sewee Creek near Decatur, Tenn. | 117 | - | 22.7 | 11.5 | 21.16 | 16.56 |
| 03556000 | Turtletown Creek at Turtletown, Tenn. | 26.9 | - | 10.5 | 25.3 | 11.95 | 8.77 |

Table 5.--Stations and drainage basin characteristics used in lagtime regression analyses--Continued

| Station No. | Name | Drainage area, DA (mi ²) | Percentage of impervious area IA, (percent) | Channel length, CL (mi) | Channel slope CS (ft/mi) | Average basin lagtime, LT (h) | Estimated lagtime from equations, LT(h) |
|----------------------------------|---|--------------------------------------|---|-------------------------|--------------------------|-------------------------------|---|
| <u>East Tennessee--Continued</u> | | | | | | | |
| 03565300 | South Chestuee Creek near Benton, Tenn. | 31.8 | - | 10.6 | 14.3 | 16.60 | 8.84 |
| 03565500 | Oostanaula Creek near Sanford, Tenn. | 57.0 | - | 40.5 | 7.49 | 27.76 | 26.70 |
| 03566420 | Wolftever Creek near Ooltewah, Tenn. | 18.8 | - | 7.80 | 16.58 | 9.92 | 6.86 |
| 03567500 | South Chickamauga Creek near Chickamauga, Tenn. | 428 | - | 46.2 | 5.58 | 40.47 | 29.76 |
| 03568500 | Chattanooga Creek near Flintstone, Ga. | 50.6 | - | 17.0 | 14.9 | 23.08 | 13.05 |
| 03571000 | Sequatchie River near Whitwell, Tenn. | 402 | - | 89.2 | 3.29 | 46.64 | 51.22 |
| 03578000 | Elk River near Pelham, Tenn. | 65.6 | - | 15.5 | 78.3 | 30.70 | 12.09 |
| <u>West Tennessee</u> | | | | | | | |
| 03606500 | Big Sandy River at Bruceton, Tenn. | 205 | - | 28.9 | 3.75 | 45.39 | 34.43 |
| 03607274 | Bailey Fork Creek Trib. at Paris, Tenn. | 1.04 | 15.60 | 2.34 | 57.1 | 1.44 | 1.01 |
| 07024300 | Beaver Creek at Huntingdon, Tenn. | 55.5 | - | 11.8 | 6.02 | 25.07 | 13.27 |
| 07024500 | South Fork Obion River near Greenfield, Tenn. | 383 | - | 37.4 | 3.81 | 83.13 | 54.34 |
| 07025500 | North Fork Obion River near Union City, Tenn. | 480 | - | 44.5 | 3.65 | 52.70 | 64.08 |
| 07026500 | Reelfoot Creek near Samburg, Tenn. | 110 | - | 24.3 | 3.72 | 16.61 | 21.86 |
| 07027500 | South Fork Forked Deer River near Jackson, Tenn. | 495 | - | 37.2 | 4.27 | 60.05 | 65.54 |
| 07027530 | South Fork Forked Deer River Trib. at Jackson, Tenn. | .98 | 39.86 | 1.64 | 54.9 | .64 | .71 |
| 07028500 | North Fork Forked Deer River near Trenton, Tenn. | 73.5 | - | 16.0 | 6.42 | 31.07 | 16.28 |
| 07028930 | Turkey Creek at Medina, Tenn. | 4.75 | - | 3.50 | 34.32 | 1.70 | 2.20 |
| 07028935 | Turkey Creek Tributary near Medina, Tenn. | 1.08 | - | 1.80 | 52.80 | 1.12 | .75 |
| 07028940 | Turkey Creek near Medina, Tenn. | 7.87 | - | 4.56 | 26.93 | 2.10 | 3.19 |
| 07028950 | Turkey Creek near Fairview, Tenn. | 13.3 | - | 6.78 | 18.48 | 2.86 | 4.68 |
| 07028985 | Middle Fork Forked Deer River Trib. at Humboldt, Tenn. | 2.12 | 25.4 | 2.64 | 26.3 | 1.84 | 1.08 |
| 07029000 | Middle Fork Forked Deer River near Alamo, Tenn. | 369 | - | 47.3 | 3.86 | 51.23 | 52.89 |
| 07030147 | Town Creek Tributary at Covington, Tenn. | .75 | 19.3 | 1.70 | 42.7 | .97 | .83 |
| 07030240 | Loosahatchie River near Arlington, Tenn. | 262 | - | 28.0 | 8.52 | 26.47 | 41.19 |
| 07030295 | Loosahatchie River Trib. at New Allen Rd. at Memphis, Tenn. | 1.26 | 11.0 | 1.87 | 43.2 | 2.369 | 1.22 |
| 07030300 | Loosahatchie River Trib. at St. Elmo Ave. at Memphis, Tenn. | .82 | 36.0 | 1.22 | 45.8 | .466 | .69 |
| 07030500 | Wolf River at Rossville, Tenn. | 503 | - | 58.9 | 3.03 | 56.64 | 66.31 |

Table 5.--Stations and drainage basin characteristics used in lagtime regression analyses--Continued

| <u>Station</u> No. | <u>Name</u> | Drainage area, DA (mi ²) | Percentage of impervious area IA, (percent) | Channel length, CL (mi) | Channel slope CS (ft/mi) | Average basin lagtime, LT (h) | Estimated lagtime from equations, LT (h) |
|----------------------------------|--|--|--|-------------------------------|--------------------------------|--|--|
| <u>West Tennessee--Continued</u> | | | | | | | |
| 07031653 | Wolf River Trib. at Willey Rd. at Germantown, Tenn. | 0.21 | 32.0 | 0.74 | 68.6 | 0.724 | 0.45 |
| 07031657 | Wolf River Trib. at Neshoba Rd. at Germantown, Tenn. | .36 | 24.0 | .83 | 52.8 | .360 | .60 |
| 07031665 | White Station Creek at Rich Rd. at Memphis, Tenn. | 2.45 | 38.0 | 2.37 | 35.5 | .627 | .99 |
| 07031680 | Fletcher Creek near Cordova, Tenn. | 1.45 | 7.0 | 2.50 | 29.1 | 2.063 | 1.51 |
| 07031690 | Fletcher Creek Trib. at Whitten Rd. at Memphis, Tenn. | .54 | 1.0 | 1.17 | 43.1 | 1.778 | 2.14 |
| 07031694 | Harrington Creek Trib. at Elmore Park Rd. at Bartlett, Tenn. | .33 | 27.0 | 1.06 | 44.0 | .716 | .56 |
| 07031695 | Harrington Creek Trib. at Hawthorne Rd. at Bartlett, Tenn. | .21 | 21.0 | .59 | 74.9 | .585 | .52 |
| 07031697 | Harrington Creek Trib. at Stage Rd. at Bartlett, Tenn. | .91 | 12.0 | 1.65 | 49.4 | .544 | 1.06 |
| 07031710 | Harrington Creek at Charles- Wood Rd. at Memphis, Tenn. | 1.59 | 38.0 | 2.12 | 28.9 | .590 | .85 |
| 07031725 | Workhouse Bayou Trib. at Isabelle St. at Memphis, Tenn. | .09 | 46.0 | .48 | 34.5 | .268 | .29 |
| 07031758 | Cypress Creek at Broad Street at Memphis, Tenn. | 4.97 | 57.8 | 4.66 | 19.1 | .86 | 1.09 |
| 07031761 | Cypress Creek Trib. at Cumberland Ave. at Memphis, Tenn. | .47 | 49.0 | 1.05 | 52.8 | .572 | .51 |
| 07031765 | Overton Bayou at North Drive at Memphis, Tenn. | .30 | 59.0 | 1.17 | 50.0 | .294 | .41 |
| 07031773 | Lick Creek at Jefferson Ave. at Memphis, Tenn. | 1.00 | 54.0 | 1.53 | 34.7 | .643 | .64 |
| 07031777 | Lick Creek at Dickinson St. at Memphis, Tenn. | 2.96 | 46.0 | 3.28 | 22.0 | .878 | .98 |
| 07031795 | Wolf River Trib. at Whitney Ave. at Memphis, Tenn. | .35 | 50.0 | .84 | 53.5 | .762 | .46 |
| 07032222 | Johns Creek Tributary at Holmes Rd. near Memphis, Tenn. | 5.83 | 4.0 | 3.11 | 26.6 | 3.080 | 2.98 |
| 07032224 | Johns Creek at Raines Road at Memphis, Tenn. | 19.4 | 5.0 | 5.64 | 18.7 | 3.644 | 4.19 |
| 07032241 | Black Bayou at Southern Ave. at Memphis, Tenn. | .59 | 49.0 | 1.14 | 27.0 | .424 | .55 |
| 07032242 | Cherry Bayou at Park Avenue at Memphis, Tenn. | .18 | 15.0 | .72 | 63.0 | .317 | .55 |
| 07032244 | Cherokee Creek at Kimball Ave. at Memphis, Tenn. | .49 | 52.0 | 1.04 | 43.5 | .494 | .50 |
| 07032246 | Days Creek at Shelby Drive at Memphis, Tenn. | 2.63 | 40.0 | 2.91 | 17.9 | 2.010 | .99 |
| 07032247 | Parkway Bayou at South Parkway East, at Memphis, Tenn. | .49 | 65.0 | 1.04 | 42.2 | .335 | .47 |
| 07032248 | Cane Creek at East Person Ave. at Memphis, Tenn. | 4.98 | 74.0 | 3.11 | 24.7 | .914 | 1.00 |
| 07032249 | Latham Branch at Valley Blvd. at Memphis, Tenn. | .043 | 69.0 | .35 | 10.4 | .265 | .20 |
| 07032260 | Cypress Creek at Neely Road at Memphis, Tenn. | 3.18 | 42.0 | 2.27 | 31.8 | 1.350 | 1.04 |

Table 6.--Summary of lagtime regression equations

| Equation | Standard error of estimate (percent) | Coefficient of determination R^2 |
|--|--|--|
| $LT = 1.26 (CL)^{0.825}$ | <u>East Tennessee</u> 47.1 | 0.83 |
| $LT = 0.707 (DA)^{0.73}$ | <u>West Tennessee</u> 42.6 | .93 |
| $LT = 2.65 (DA)^{0.348} (IA)^{-0.357}$ | 38.6 | .75 |

LT is estimated basin lagtime, in hours;
CL is channel length, in miles;
DA is drainage basin size, in square miles; and
IA is percentage of contributing drainage basin with impervious surface.

range of the basins used in the lagtime regression analyses are summarized in the following tables.

| RURAL | | | URBAN | |
|---|---------------------------------|-------------------|---|---------------------------------|
| Range in drainage area size (mi ²) | Number of basins in analysis | | Range in drainage area size (mi ²) | Number of basins in analysis |
| | East Tennessee | West Tennessee | | West Tennessee |
| 1.08 - 5.00 | 11 | 2 | 0.043 - 0.10 | 2 |
| 5.01 - 15.0 | 3 | 2 | .11 - 1.00 | 17 |
| 5.01 - 50.0 | 6 | 0 | 1.01 - 5.00 | 11 |
| 50.01 - 200 | 10 | 3 | 5.01 - 10.0 | 1 |
| 201 - 350 | 2 | 2 | 10.1 - 19.4 | 1 |
| 351 - 518 | 4 | 5 | | |
| Total | 36 | 14 | Total | 32 |

The following tables summarize the distribution of channel length for basins used in the lagtime regression equations.

| RURAL | | | URBAN | |
|---------------------------------|---------------------------------|-------------------|---------------------------------|---------------------------------|
| Range in channel length (mi) | Number of basins in analysis | | Range in channel length (mi) | Number of basins in analysis |
| | East Tennessee | West Tennessee | | West Tennessee |
| 1.00 - 2.00 | 4 | 1 | 0.35 - 1.00 | 7 |
| 2.01 - 4.20 | 7 | 1 | 1.01 - 2.00 | 13 |
| 4.21 - 9.00 | 5 | 2 | 2.01 - 3.00 | 7 |
| 9.01 - 25.0 | 9 | 3 | 3.01 - 4.00 | 3 |
| 25.1 - 45.0 | 7 | 5 | 4.01 - 5.64 | 2 |
| 45.1 - 90.0 | 4 | 2 | | |
| Total | 36 | 14 | Total | 32 |

The following table summarizes the distribution of impervious area for the basins used in West Tennessee.

| URBAN | | |
|---------------------------------------|--------|-----------------------------------|
| Range in impervious area (percent) | | Number of stations in analysis |
| 1.00 | - 10.0 | 4 |
| 10.1 | - 15.0 | 3 |
| 15.1 | - 30.0 | 6 |
| 30.1 | - 40.0 | 6 |
| 40.1 | - 50.0 | 6 |
| 50.1 | - 74.0 | 7 |
| Total | | 32 |

The log-linear form of the estimating equations was checked with graphical plots. Plots of regression residuals versus observed lagtime, and versus each of the independent variables were made. The scatter of plotting points on each graph appeared to be random with no apparent bias. Therefore, the form of the estimating equation is assumed to be appropriate.

It should be noted that the urban basin lagtime equation for West Tennessee may predict a longer lagtime than the rural basin lagtime equation. Conceptually, this should not occur because increasing imperviousness should decrease lagtime. Therefore, when estimating lagtime for urbanized basins, lagtime should be calculated from both equations, and the smallest value should probably be used.

Station residuals were plotted on a map to evaluate geographic bias of estimates from the rural and urban basin lagtime equations. Although the residuals varied considerably between stations, no specific geographic trends could be detected. Due to the limited number of stations available, verification of the regression equations was not possible.

A partial analysis of the sensitivity of the lagtime equations to the dependent variables was performed. Results of this analysis are shown graphically in figures 8 and 9. For example in

East Tennessee, an error of plus 20 percent in computing channel length results in about a plus 16 percent difference in lagtime. For the urban basin lagtime equation for West Tennessee, an error of plus 20 percent in computing drainage area results in about a plus 7 percent difference in lagtime, and an error of minus 20 percent in computing the percentage of impervious area results in about a plus 8 percent difference in lagtime.

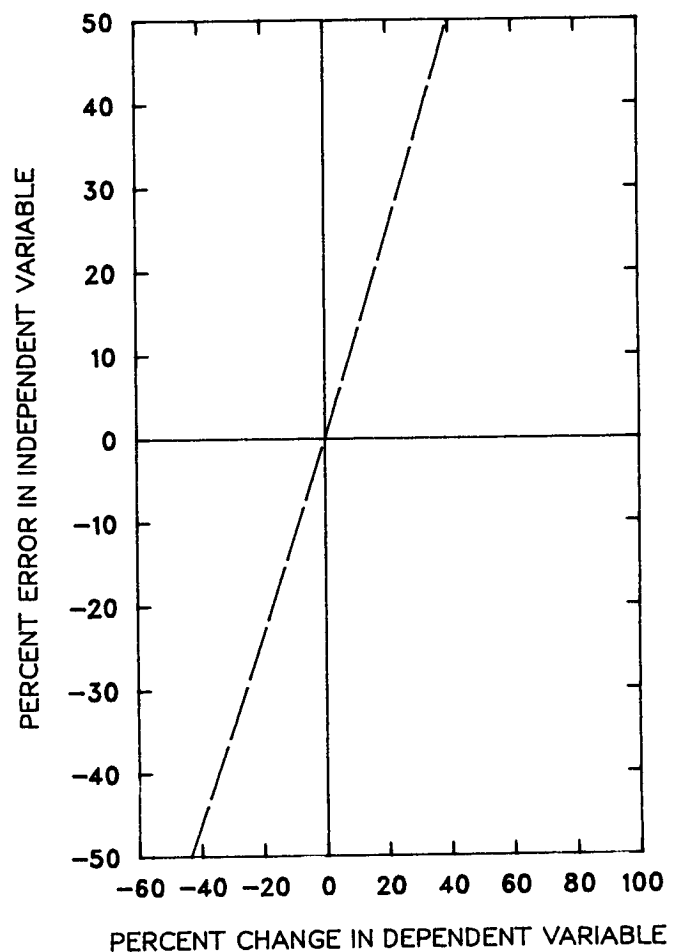


Figure 8.--Percent change in lagtime for rural streams in East Tennessee resulting from errors in computing channel length.

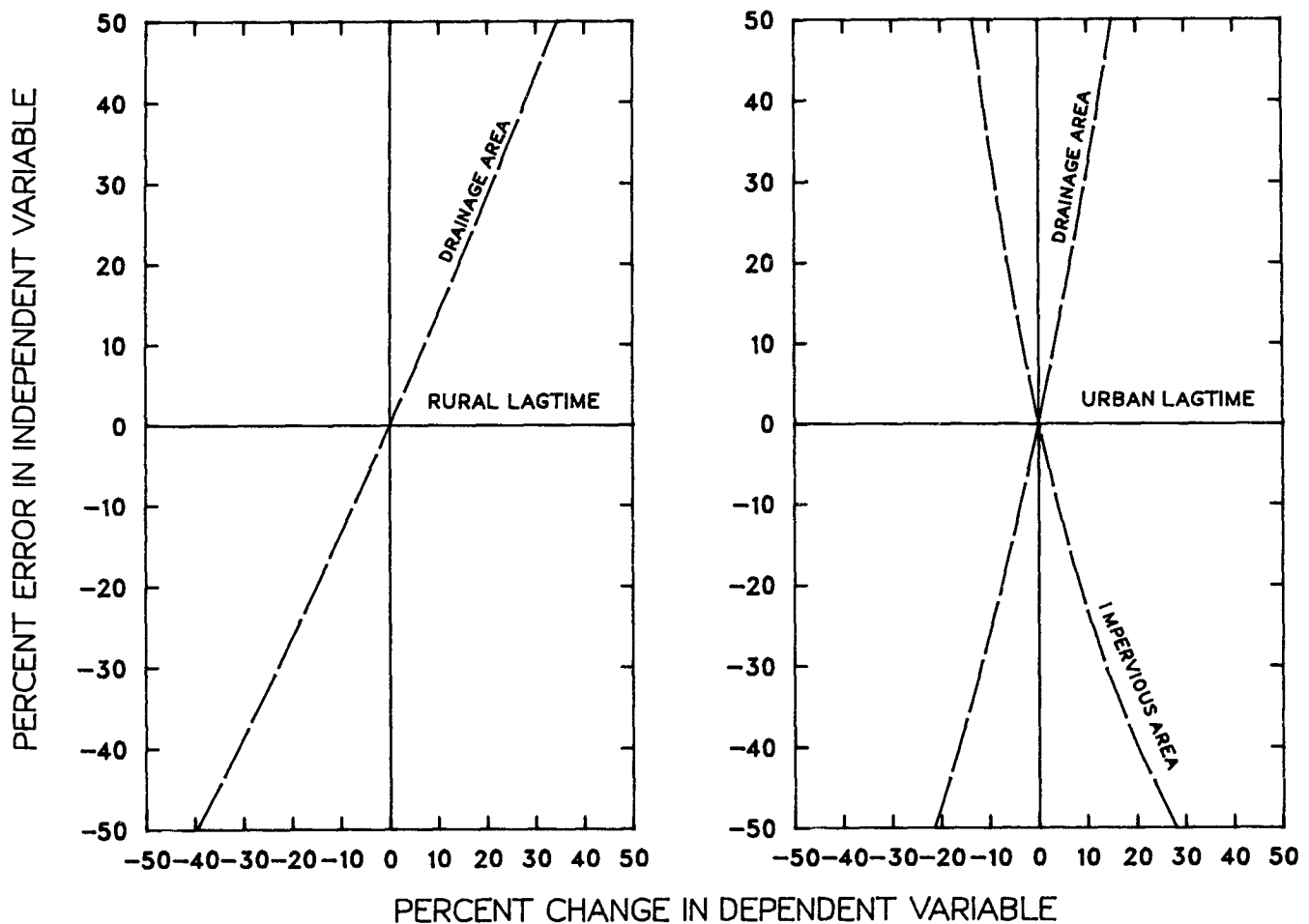


Figure 9.--Percent change in lagtime for rural and urban streams in West Tennessee resulting from errors in computing drainage area and percentage of impervious area.

Estimating Flood Volume

Storage of floodwater or flood detention may often be part of a particular structure's design. In such cases, it is important to know the volume of flood runoff associated with the design flood. Therefore, an equation for estimating flood volume for selected recurrence interval floods on East and West Tennessee streams was developed. The equation relates flood volume to drainage area size, flood peak discharge, and basin lagtime. Observed flood volumes (in inches of runoff), obtained as part of the unit hydrograph computations discussed earlier were used in this analysis.

Regression Analyses

Stepwise regression techniques were used with three basin characteristics to derive the equations for estimating flood volumes (table 7). These equations may be used for estimating flood volumes associated with a given T-year peak discharge for ungaged streams in East and West Tennessee. Flood volume can also be obtained by summing the ordinates of the estimated flood hydrograph. The three basin characteristics, drainage basin size, flood peak discharge, and basin lagtime, were all statistically significant at the 95-percent confidence level. The drainage area size range for stations used in

Table 7.--Summary of volume regression equations

| Equation | Standard error of estimate (percent) | Coefficient of determination R^2 |
|---|--------------------------------------|------------------------------------|
| $\text{Vol} = 0.00234 (\text{DA})^{-0.953} (\text{Qp})^{0.947} (\text{LT})^{0.956}$ <u>East Tennessee</u> | 22.1 | 0.95 |
| $\text{Vol} = 0.0035 (\text{DA})^{-0.881} (\text{Qp})^{0.866} (\text{LT})^{0.968}$ <u>West Tennessee</u> | 23.9 | .91 |

Vol is estimated flood volume, in inches;
DA is drainage area, in square miles;
Qp is flood peak discharge, in cubic feet per second; and
LT is basin lagtime, in hours.

the regression analysis was 1.10 to 518 mi² for East Tennessee and 1.08 to 503 mi² for West Tennessee and had distribution as shown in the following table.

| Range in drainage area size (mi ²) | Number of storms in analysis* | |
|--|-------------------------------|----------------|
| | East Tennessee | West Tennessee |
| 1.08 - 5.0 | 29 | 8 |
| 5.1 - 10.0 | 0 | 6 |
| 10.1 - 20.0 | 10 | 4 |
| 20.1 - 50.0 | 10 | 0 |
| 50.1 - 100.0 | 23 | 7 |
| 101.0 - 300.0 | 28 | 10 |
| 301.0 - 518.0 | 18 | 21 |
| Totals | 118 | 56 |

*More than one storm per station was used.

Flood peak discharges ranged from 50.2 to 36,000 ft³/s for East Tennessee and 163 to 23,600 ft³/s for West Tennessee and had distribution as shown in the following table.

| Range in flood-peak discharge (ft ³ /s) | Number of storms in analysis* | |
|--|-------------------------------|----------------|
| | East Tennessee | West Tennessee |
| 50.2 - 100 | 5 | - |
| 101 - 500 | 25 | 4 |
| 501 - 1,000 | 5 | 5 |
| 1,001 - 4,000 | 35 | 18 |
| 4,001 - 10,000 | 25 | 22 |
| 10,001 - 20,000 | 17 | 5 |
| 20,001 - 36,000 | 6 | 2 |
| Totals | 118 | 56 |

*More than one storm per station was used.

Average basin lagtimes for East Tennessee ranged from 1.55 to 46.64 hours and for West Tennessee from 1.47 to 84.05 hours. The following table summarizes the distribution of lagtimes for the basins used.

| Range in basin lagtime, in hours | Number of storms in analysis* | |
|----------------------------------|-------------------------------|----------------|
| | East Tennessee | West Tennessee |
| 1.47 - 2.00 | 11 | 4 |
| 2.01 - 5.00 | 15 | 14 |
| 5.01 - 10.00 | 10 | 0 |
| 10.01 - 20.00 | 41 | 3 |
| 20.01 - 30.00 | 29 | 6 |
| 30.01 - 50.00 | 12 | 8 |
| 50.01 - 70.00 | 0 | 16 |
| 70.01 - 84.05 | 0 | 5 |
| Totals | 118 | 56 |

*More than one storm per station was used.

The log-linear form of the estimating equation was verified with graphical plots. Plots of regression residuals versus drainage area, flood peak discharge, and basin lagtime were made. The scatter of plotting points on each graph appeared to be random with no apparent bias. Therefore, the form of the estimating equation is assumed to be appropriate.

Station residuals were plotted on a map to evaluate geographic bias of estimates from the flood-volume equation. Although the residuals varied between stations, no geographic trends could be detected.

A partial analysis of the sensitivity of the volume equations to drainage area, flood peak discharge, and basin lagtime was performed, and the results are shown graphically in figures 10 and 11. Results for East Tennessee indicate that an error of minus 20 percent in computing drainage area, for example, results in about a 24-percent difference in flood volume; and an error of 20 percent each in computing flood peak discharge and basin lagtime results in about a 19- and 19-percent error in flood volume, respectively. In West Tennessee, an error of minus 20 percent in computing drainage area results in about a plus 22-percent error in flood volume; and an error of 20 percent each in computing

flood peak discharge and basin lagtime results in about a 17- and 19-percent error in flood volume, respectively.

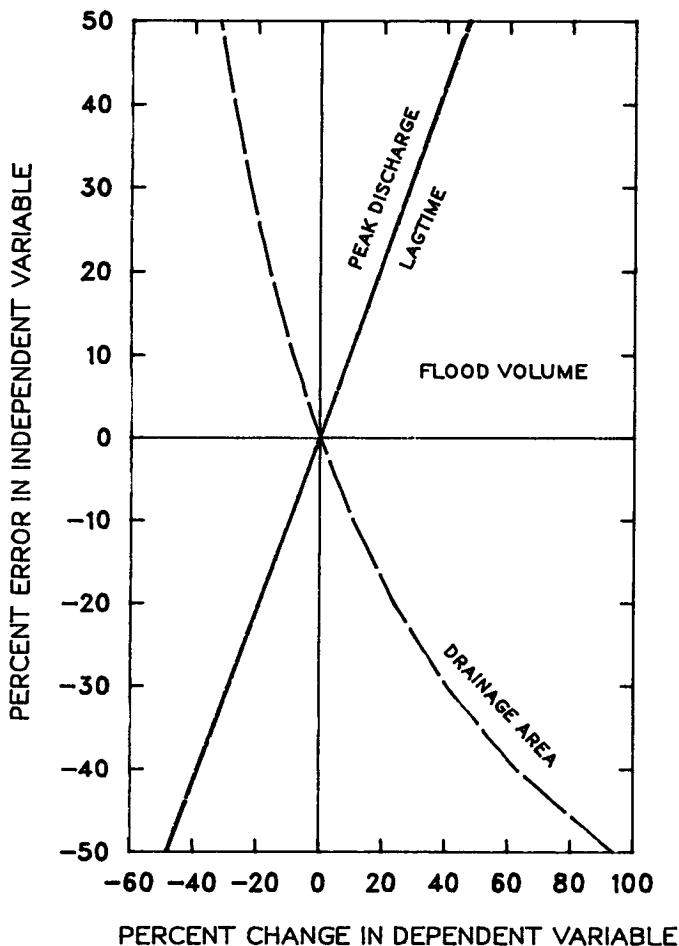


Figure 10.--Percent change in flood volume for streams in East Tennessee resulting from errors in computing drainage area, lagtime, and peak discharge.

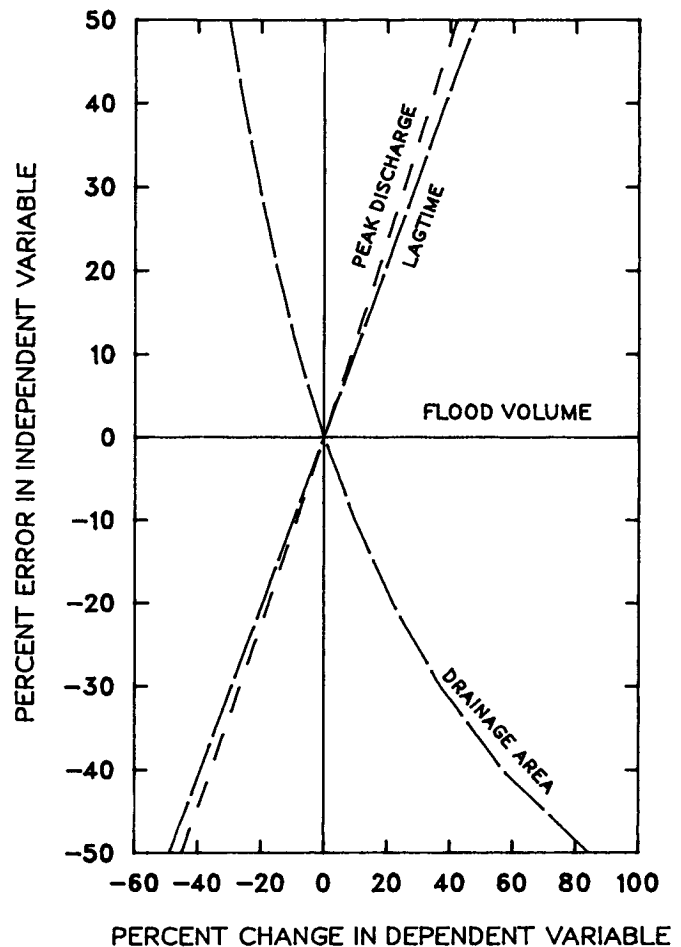


Figure 11.--Percent change in flood volume for streams in West Tennessee resulting from errors in computing drainage area, lagtime, and peak discharge.

Alternate Flood-Volume Equation

An alternate flood-volume equation developed by Sauer (written communication, 1987) can also be used to compute the volume of runoff, in inches, from an estimated storm hydrograph. The values produced by this alternate equation equal the values that would be obtained by summing the ordinates of the flood hydrograph and converting to inches of runoff. This equation is:

$$\text{Vol} = \frac{a(\text{PQ})(\text{LT})}{(\text{DA})}$$

where

Vol is estimated flood volume, in inches;
PQ is flood peak discharge, in cubic feet per second;
LT is basin lagtime, in hours;
DA is drainage area, in square miles; and
a is a conversion constant.

The theoretical value of "a" is 0.00155; however, "a" should be computed from the dimensionless hydrograph for the area in which the basin is located where runoff is desired. The computations involve summing the ordinates of the dimensionless hydrograph and converting to inches of runoff for 1 square mile. The value of "a" for East Tennessee has been computed as 0.00169 and for West Tennessee, 0.00218.

Flood volumes have been computed using the above equation for the same stations and storms as was used to develop the regression equations given in the previous section. The standard error of the equation when applied to the East Tennessee data is 17.8 percent and for West Tennessee is 33.1 percent.

Flood volumes may be computed by the above equation, by the regression equations given in the previous section, or by summing the ordinates of the computed flood hydrograph. Summing the ordinates gives the most accurate results, but the equations are easier to apply. The user must balance accuracy against effort in choosing the method to be used.

HYDROGRAPH-WIDTH RELATION

For some hydraulic analyses, it is necessary to estimate the period of time that a specific discharge will be exceeded. In order to estimate this time period, a hydrograph-width relation was defined for the dimensionless hydrographs of East and West Tennessee. Hydrograph-width

ratios were determined by subtracting the value of t/LT on the rising limb of the dimensionless hydrograph from the value of t/LT on the falling limb of the hydrograph at the same discharge ratio (Q_t/Q_p) over the full range of the dimensionless hydrograph. The resulting hydrograph-width relations are listed in table 8 and are shown graphically in figure 12. The simulated hydrograph width (W) in hours can be estimated for a specified discharge (Q_t) by first computing the ratio Q_t/Q_p and then multiplying the corresponding W/LT ratio in table 3 (or figure 8) by the estimated basin lagtime (LT). The resulting hydrograph width is the period of time the specified discharge will be exceeded.

APPLICATION OF HYDROGRAPH SIMULATION TECHNIQUE

A step-by-step procedure is described below to assist the user in applying the techniques for simulating flood hydrographs and estimating flood volumes and hydrograph widths as presented in this report. In addition, an example is given to demonstrate these techniques. The procedure is as follows:

1. Determine the drainage area and main-channel length of the basin from the best available topographic maps.
2. Compute the peak discharge for the desired recurrence-interval flood from the applicable flood-frequency report (flood-frequency equations included in Supplemental Information).
3. Estimate percentage of impervious area if the basin is urbanized.
4. Compute the basin lagtime from the appropriate equation (table 6).
5. Compute the coordinates of the flood hydrograph by multiplying the value of

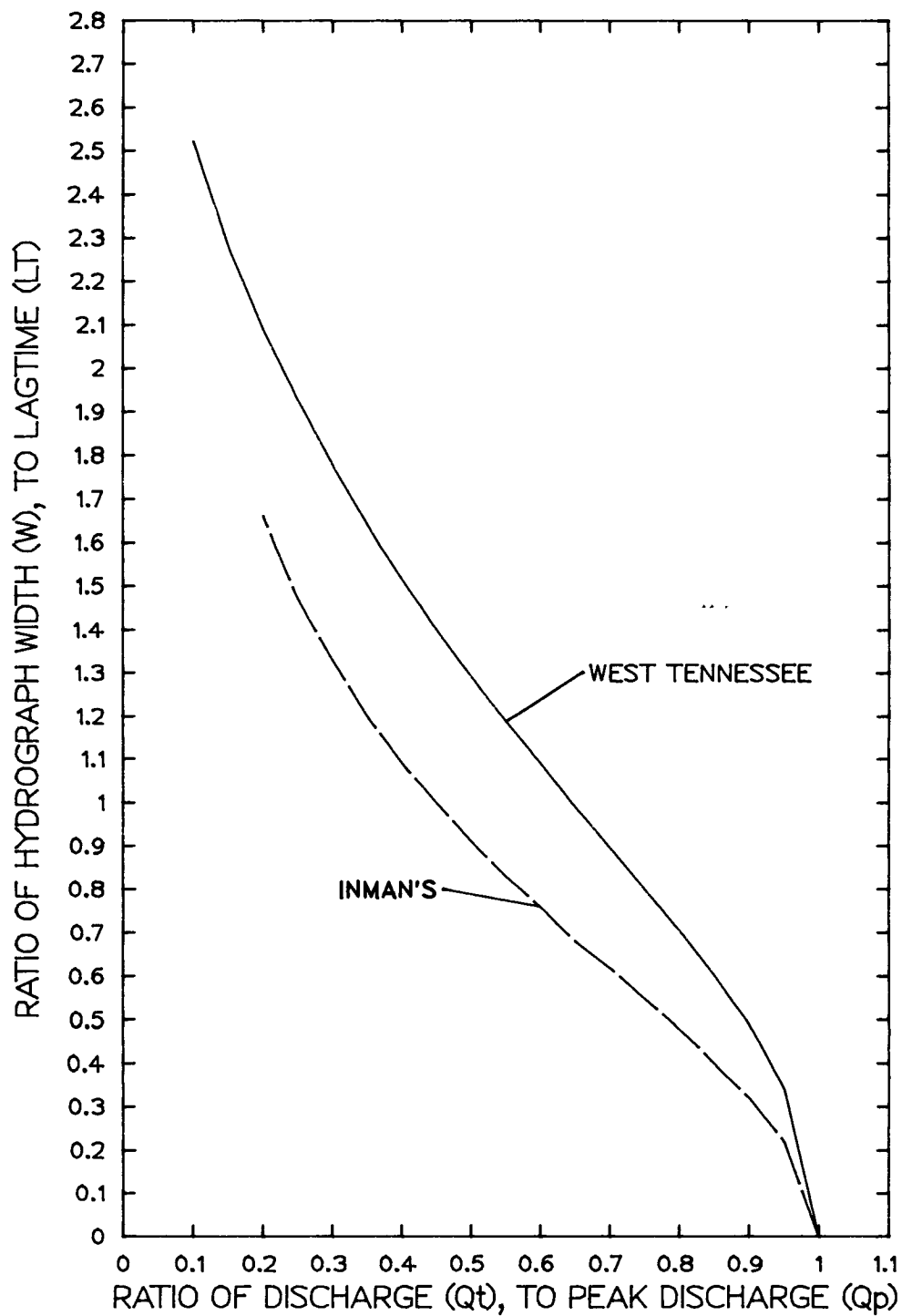


Figure 12. — Hydrograph-width relation for West Tennessee and Inman's dimensionless hydrographs.

Table 8.--*Discharge and hydrograph-width ratios for East and West Tennessee dimensionless hydrographs*

[Data for East Tennessee modified from Inman (1986)]

| Discharge ratios Q_t/Q_p | East Tennessee Width ratios W/LT | West Tennessee Width ratios W/LT |
|-------------------------------|---|---|
| 1.00 | 0 | 0 |
| .95 | .22 | .34 |
| .90 | .32 | .49 |
| .85 | .40 | .60 |
| .80 | .48 | .70 |
| .75 | .55 | .80 |
| .70 | .62 | .90 |
| .65 | .68 | .99 |
| .60 | .76 | 1.09 |
| .55 | .83 | 1.19 |
| .50 | .91 | 1.29 |
| .45 | 1.00 | 1.40 |
| .40 | 1.09 | 1.52 |
| .35 | 1.20 | 1.64 |
| .30 | 1.33 | 1.78 |
| .25 | 1.47 | 1.93 |
| .20 | 1.66 | 2.09 |
| .15 | -- | 2.28 |
| .10 | -- | 2.52 |

lagtime by the time ratios and the value of peak discharge by the discharge ratios of the appropriate dimensionless hydrograph (table 2 or 3).

6. Compute the volume for the selected recurrence-interval flood using the appropriate equation from table 7.
7. Compute the period of time a specific discharge will be exceeded using the appropriate dimensionless hydrograph-width relation (table 8, or figure 12).

Limitations

The techniques for simulating flood hydrographs and estimating flood volumes described in this report are limited to streams in hydrologic areas 1 and 4 (East Tennessee and West Tennessee, respectively) as defined by Randolph and

Gamble (1976). The size range for the data used in deriving the equations given in this report are as follows:

RURAL LAGTIME

| East Tennessee channel length (mi) | West Tennessee basin size (mi ²) |
|--|--|
| 1.19 - 89.2 | 1.08 - 503 |

URBAN LAGTIME (West Tennessee)

| Basin size (mi ²) | Impervious area (percent) |
|----------------------------------|------------------------------|
| 0.043 - 19.4 | 1.0 - 74 |

FLOOD VOLUME

| Peak discharge (ft ³ /s) | East Tennessee Basin size (mi ²) | Basin lagtime (hours) |
|--|--|--------------------------|
| | 1.10 - 518 | |
| 50.2 - 36,000 | | 1.55 - 46.64 |
| 163 - 23,600 | West Tennessee 1.08 - 503 | 1.47 - 84.05 |
| | | |

Use of the hydrograph simulation technique and regression equations should be limited to these ranges because the techniques presented have not been tested beyond the indicated range in values. If sites with values outside these ranges are used, the standard error may be considerably higher than for sites where all variables

are within the range shown above. In addition, these techniques should not be applied to streams where temporary in-channel storage or overbank detention storage is significant unless suitable estimates of peak discharge and lagtime are available which account for these effects.

Example Problem

The following example illustrates the procedure for computing the simulated hydrograph and flood volume associated with the 50-year discharge estimate in a hypothetical rural basin in hydrologic area 1 in East Tennessee.

1. The drainage area (DA) is determined as 47.3 mi² and the main-channel length is determined to be 20.1 miles.
2. The peak discharge (Q_{50}) for the 50-year recurrence-interval flood is 6,940 ft³/s (Randolph and Gamble, 1976--in supplement).
3. Using the rural lagtime equation for East Tennessee shown in table 6, the basin lagtime (LT) is estimated to be:

$$\begin{aligned} LT &= 1.26 (CL)^{0.825} \\ &= 1.26 (20.1)^{0.825} \\ &= 15.0 \text{ hours} \end{aligned}$$

4. The coordinates of the simulated flood hydrograph are listed below and are shown graphically in figure 13:

| t/LT (from table 2) | X | LT (from step 3) | = | time (h) | Q _t /Q _p (from table 2) | X | Q _p (from step 2) | = | Discharge (ft ³ /s) |
|---------------------------|---|------------------------|---|-------------|---|---|------------------------------------|---|-----------------------------------|
| 0.25 | | 15.0 | | 3.8 | 0.12 | | 6,940 | | 833 |
| .30 | | 15.0 | | 4.5 | .16 | | 6,940 | | 1,110 |
| .35 | | 15.0 | | 5.2 | .21 | | 6,940 | | 1,460 |
| .40 | | 15.0 | | 6.0 | .26 | | 6,940 | | 1,800 |
| .45 | | 15.0 | | 6.8 | .33 | | 6,940 | | 2,290 |
| .50 | | 15.0 | | 7.5 | .40 | | 6,940 | | 2,780 |
| .55 | | 15.0 | | 8.2 | .49 | | 6,940 | | 3,400 |
| .60 | | 15.0 | | 9.0 | .58 | | 6,940 | | 4,020 |
| .65 | | 15.0 | | 9.8 | .67 | | 6,940 | | 4,650 |
| .70 | | 15.0 | | 10.5 | .76 | | 6,940 | | 5,270 |
| .75 | | 15.0 | | 11.2 | .84 | | 6,940 | | 5,830 |
| .80 | | 15.0 | | 12.0 | .90 | | 6,940 | | 6,250 |
| .85 | | 15.0 | | 12.8 | .95 | | 6,940 | | 6,590 |
| .90 | | 15.0 | | 13.5 | .98 | | 6,940 | | 6,800 |
| .95 | | 15.0 | | 14.2 | 1.00 | | 6,940 | | 6,940 |
| 1.00 | | 15.0 | | 15.0 | .99 | | 6,940 | | 6,870 |
| 1.05 | | 15.0 | | 15.8 | .96 | | 6,940 | | 6,660 |
| 1.10 | | 15.0 | | 16.5 | .92 | | 6,940 | | 6,380 |
| 1.15 | | 15.0 | | 17.2 | .86 | | 6,940 | | 5,970 |
| 1.20 | | 15.0 | | 18.0 | .80 | | 6,940 | | 5,550 |
| 1.25 | | 15.0 | | 18.8 | .74 | | 6,940 | | 5,140 |
| 1.30 | | 15.0 | | 19.5 | .68 | | 6,940 | | 4,720 |
| 1.35 | | 15.0 | | 20.2 | .62 | | 6,940 | | 4,300 |
| 1.40 | | 15.0 | | 21.0 | .56 | | 6,940 | | 3,890 |
| 1.45 | | 15.0 | | 21.8 | .51 | | 6,940 | | 3,540 |
| 1.50 | | 15.0 | | 22.5 | .47 | | 6,940 | | 3,260 |
| 1.55 | | 15.0 | | 23.2 | .43 | | 6,940 | | 2,980 |
| 1.60 | | 15.0 | | 24.0 | .39 | | 6,940 | | 2,710 |
| 1.65 | | 15.0 | | 24.8 | .36 | | 6,940 | | 2,500 |
| 1.70 | | 15.0 | | 25.5 | .33 | | 6,940 | | 2,290 |
| 1.75 | | 15.0 | | 26.2 | .30 | | 6,940 | | 2,080 |
| 1.80 | | 15.0 | | 27.0 | .28 | | 6,940 | | 1,940 |
| 1.85 | | 15.0 | | 27.8 | .26 | | 6,940 | | 1,800 |
| 1.90 | | 15.0 | | 28.5 | .24 | | 6,940 | | 1,670 |
| 1.95 | | 15.0 | | 29.2 | .22 | | 6,940 | | 1,530 |
| 2.00 | | 15.0 | | 30.0 | .20 | | 6,940 | | 1,390 |
| 2.05 | | 15.0 | | 30.8 | .19 | | 6,940 | | 1,320 |
| 2.10 | | 15.0 | | 31.5 | .17 | | 6,940 | | 1,180 |
| 2.15 | | 15.0 | | 32.2 | .16 | | 6,940 | | 1,110 |
| 2.20 | | 15.0 | | 33.0 | .15 | | 6,940 | | 1,040 |
| 2.25 | | 15.0 | | 33.8 | .14 | | 6,940 | | 972 |
| 2.30 | | 15.0 | | 34.5 | .13 | | 6,940 | | 902 |
| 2.35 | | 15.0 | | 35.2 | .12 | | 6,940 | | 833 |
| 2.40 | | 15.0 | | 36.0 | .11 | | 6,940 | | 763 |

5. Using the volume equation for East Tennessee shown in table 7, the flood volume in inches, of the 50-year flood is:

$$\begin{aligned}
 \text{Vol} &= 0.00234 (\text{DA})^{-0.953} (\text{PQ})^{0.947} (\text{LT})^{0.956} \\
 &= 0.00234 (47.3)^{-0.953} (6,940)^{0.947} (15.0)^{0.956} \\
 &= 3.43 \text{ inches}
 \end{aligned}$$

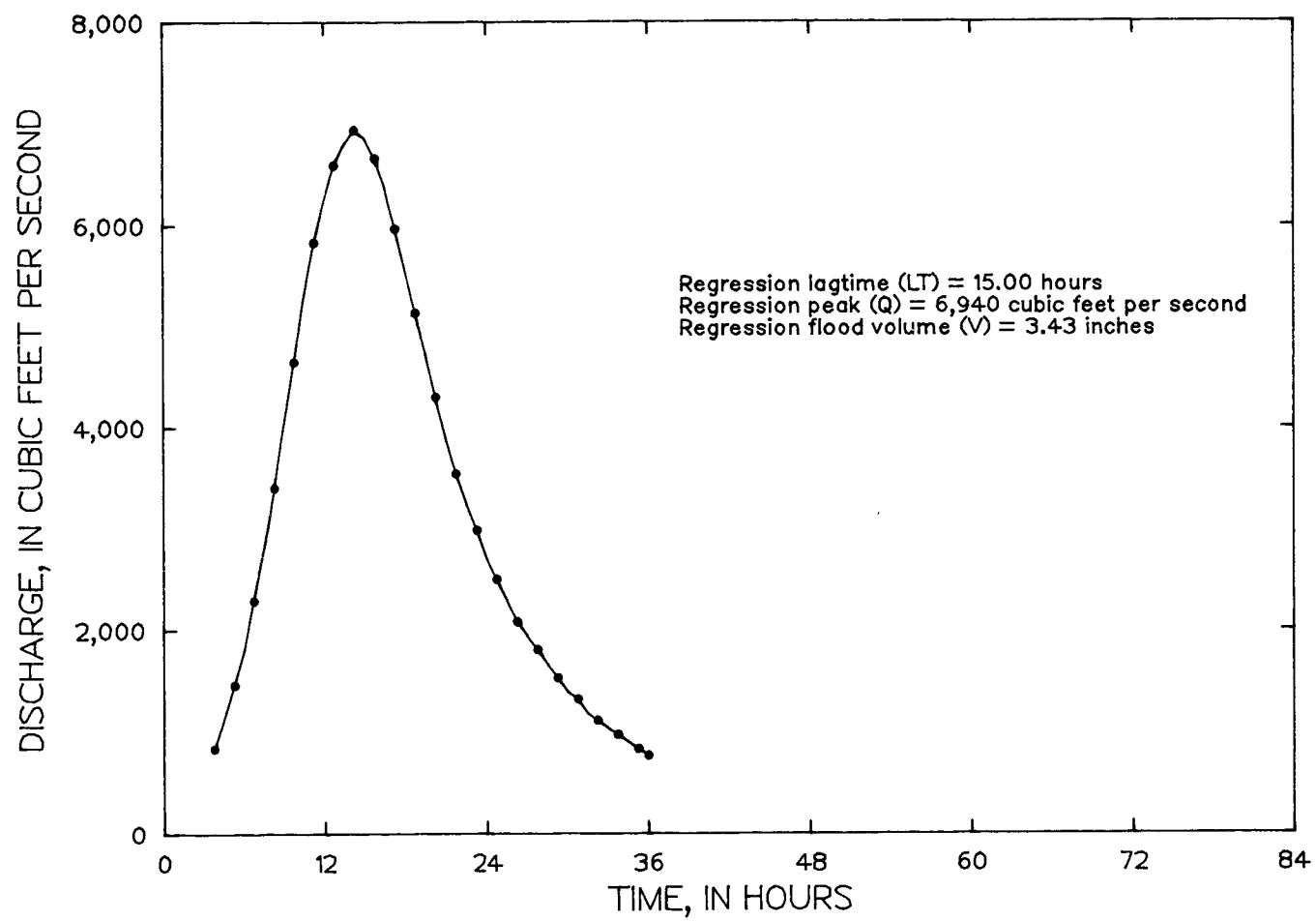


Figure 13. — Example of simulated 50-year flood hydrograph for a hypothetical river in East Tennessee.

6. If an estimate is needed for the period of time the discharge will exceed 4,500 ft³/s, compute as follows:
- a. $Q_v/Q_p = 4,500/6,940 = 0.65$
 - b. From table 8 or figure 12, $W/LT = 0.68$
 - c. Estimated basin lagtime (LT) = 15 hours, from step 3
 - d. Time 4,500 ft³/s will be exceeded $= (W/LT)(LT)$
 $= (0.68)(15.0)$
 $= 10.2 \text{ hours}$

CONCLUSIONS

A dimensionless hydrograph developed for Georgia streams was tested for its applicability to East and West Tennessee streams by comparing it to dimensionless hydrographs developed for those areas. Test results indicate the dimensionless hydrograph developed for East Tennessee is essentially the same as that developed for Georgia streams but the dimensionless hydrograph developed for West Tennessee is different (wider). Therefore, the Georgia dimensionless hydrograph can be used to simulate flood hydrographs at ungaged sites in East Tennessee. The dimensionless hydrograph developed from data for West Tennessee streams should be used to simulate flood hydrographs at ungaged sites in West Tennessee.

Multiple-regression techniques were used to develop relations between basin lagtime and selected basin characteristics. In East Tennessee, the most significant basin characteristic for rural basins was channel length. The paucity of data on urban streams in East Tennessee prevented development of an urban lagtime equation for East Tennessee urban streams. In West Tennessee, the most significant basin characteristic for rural streams was drainage basin size and for urban streams, drainage basin size and percentage of impervious area. Tests indi-

cated no geographical bias in any of the lagtime equations. For urban basins in Shelby County, it is recommended that the equation developed by Neely (1984) be used to estimate lagtime (see Supplemental Information).

An equation for estimating flood volumes was also developed for both East and West Tennessee using multiple-regression techniques. Drainage area, flood peak discharge, and basin lagtime were the significant variables in both volume equations. Tests indicated no variable or geographic bias in the volume equations. An alternate flood-volume equation is also given which uses the above variables and a derived conversion constant. The user may use either equation to compute flood volume or sum the ordinates of the estimated flood hydrograph.

A simulated flood hydrograph can be computed by applying lagtime, obtained from the appropriate regression equation, and peak discharge of a specific recurrence interval, to the dimensionless hydrograph time and discharge ratios in table 2 or 3. The coordinates of the simulated flood hydrograph are computed by multiplying lagtime by the time ratios and peak discharge by the discharge ratios. The volume of the simulated flood hydrograph can be estimated from the appropriate volume regression equation.

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SYMBOLS, DEFINITIONS, AND UNITS

| <i>Symbols</i> | <i>Definition</i> | <i>Units</i> |
|----------------|---|--------------------|
| CL | Channel length measured from the point of interest on a stream along the water course upstream to the basin divide. | mi |
| CS | Main-channel slope, computed as the difference in elevations (in feet) at points 10 and 85 percent of the distance along the main channel from the point of interest to the topographic divide, divided by the channel distance (in miles) between the two points, as determined from topographic maps. | ft/mi |
| CL/\sqrt{CS} | Ratio of channel length to the square root of channel slope. | --- |
| DA | Contributing drainage area of a basin | mi ² |
| IA | Impervious area, computed as the percent of the basin area that is covered by paved roads, paved parking lots, roofs, driveways, sidewalks, etc. | percent |
| LT | Basin lagtime, computed as the elapsed time from the centroid of rainfall excess to the centroid of the resultant runoff hydrograph. | h |
| P2_24 | 2-year 24-hour rainfall, defined as the 24-hour rainfall total having a recurrence interval of 2 years determined from U.S. Department of Commerce (1961) and shown in figure 14 of this report. | in. |
| Q_p | Flood peak discharge, defined as the maximum discharge of an observed or simulated flood hydrograph. | ft ³ /s |
| Q_t | Discharge occurring at time t | ft ³ /s |

SYMBOLS, DEFINITIONS, AND UNITS--*Continued*

| <i>Symbols</i> | <i>Definitions</i> | <i>Units</i> |
|---------------------------|--|--------------------|
| Q_t/Q_p | Ratio of discharge occurring at time t to flood peak discharge. | --- |
| $Q_{2,5,10,25,50,100}$ | Rural basin flood-frequency discharge for recurrence intervals of 2 through 100-years, respectively. | ft ³ /s |
| $Q_{(u)2,5,10,25,50,100}$ | Urban basin flood-frequency discharge for recurrence intervals of 2 through 100-years, respectively. | ft ³ /s |
| R^2 | Coefficient of determination | --- |
| t/LT | Ratio of instantaneous time to basin lagtime | --- |
| V | Flood volume | in. |
| W | Hydrograph width | h |
| W/LT | Ratio of hydrograph width to basin lagtime | --- |

SUPPLEMENTAL INFORMATION

REGIONAL FLOOD-FREQUENCY EQUATIONS FOR RURAL BASINS IN TENNESSEE

The following is a list of the rural basin flood-frequency equations from Randolph and Gamble (1976) for hydrologic areas 1 and 4.

Hydrologic Area 1

$$\begin{aligned}Q_2 &= 127(DA)^{0.752} \\Q_5 &= 211(DA)^{0.753} \\Q_{10} &= 276(DA)^{0.727} \\Q_{25} &= 366(DA)^{0.719} \\Q_{50} &= 442(DA)^{0.714} \\Q_{100} &= 524(DA)^{0.709}\end{aligned}$$

Hydrologic Area 4

$$\begin{aligned}Q_2 &= 405(DA)^{0.515} \\Q_5 &= 562(DA)^{0.540} \\Q_{10} &= 664(DA)^{0.551} \\Q_{25} &= 789(DA)^{0.563} \\Q_{50} &= 883(DA)^{0.569} \\Q_{100} &= 975(DA)^{0.575}\end{aligned}$$

Where Q_{25} is the 25-year recurrence-interval flood, in cubic feet per second; and DA is contributing drainage area, in square miles.

REGIONAL FLOOD-FREQUENCY EQUATIONS FOR URBAN BASINS IN TENNESSEE

The following is a list of the urban basin flood-frequency equations from Robbins (1984) which are applicable statewide except for Memphis and Shelby County, for which flood-frequency equations have been defined by Neely (1984) (see below). The precipitation factor (P2_24) used in each equation can be determined from figure 14.

$$\begin{aligned} Q_{(u)2} &= 1.76(DA)^{0.74} (IA)^{0.48} (P2_24)^{3.01} \\ Q_{(u)5} &= 5.55(DA)^{0.75} (IA)^{0.44} (P2_24)^{2.53} \\ Q_{(u)10} &= 11.8(DA)^{0.75} (IA)^{0.43} (P2_24)^{2.12} \\ Q_{(u)25} &= 21.9(DA)^{0.75} (IA)^{0.39} (P2_24)^{1.89} \\ Q_{(u)50} &= 44.9(DA)^{0.75} (IA)^{0.40} (P2_24)^{1.42} \\ Q_{(u)100} &= 77.0(DA)^{0.75} (IA)^{0.40} (P2_24)^{1.10} \end{aligned}$$

Where

$Q_{(u)25}$ is the 25-year recurrence-interval flood, in cubic feet per second;

DA is contributing drainage area, in square miles;

IA is percentage of the contributing drainage basin occupied by impervious surface; and

P2_24 is the 2-year 24-hour rainfall amount, in inches.

The following is a list of the urban basin flood-frequency equations from Neely (1984) which are applicable to Memphis and Shelby County.

$$\begin{aligned} Q_2 &= 488 A^{0.81} P^{1.11} \\ Q_5 &= 738 A^{0.80} P^{1.09} \\ Q_{10} &= 918 A^{0.79} P^{1.08} \\ Q_{25} &= 1,160 A^{0.78} P^{1.06} \\ Q_{50} &= 1,350 A^{0.77} P^{1.05} \\ Q_{100} &= 1,550 A^{0.76} P^{1.04} \end{aligned}$$

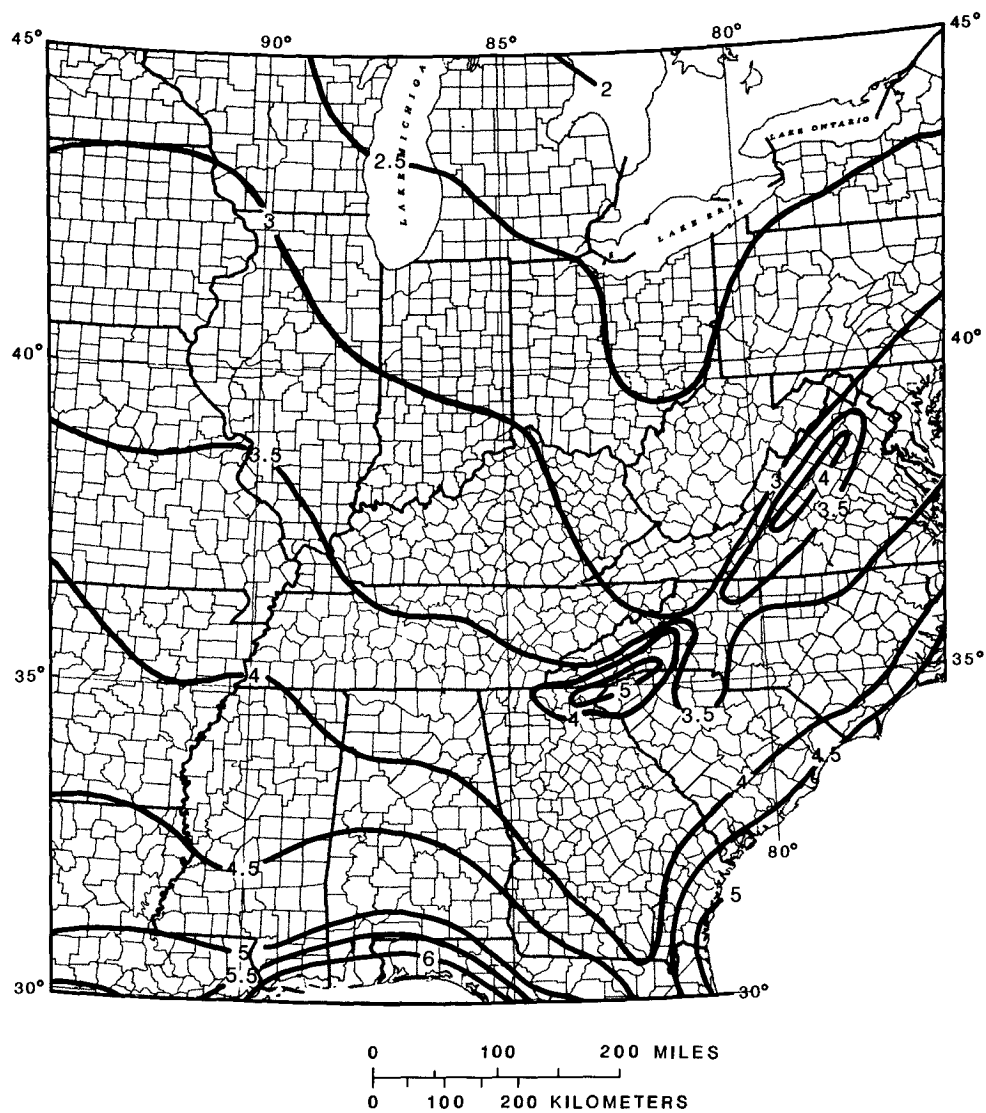
where

Q_{25} is the estimated discharge, in cubic feet per second, for the 25-year recurrence-interval flood;

A is the drainage area, in square miles; and

P is the average channel condition.

The channel condition, P, is defined and computed as follows: The average channel condition between points along the main channel at 100 percent, 75 percent, 50 percent, and 25 percent of the drainage area. If the channel is paved with concrete, use a value of 2; if unpaved, use a value of 1. Estimate the channel condition for partial paving between 1 and 2.



EXPLANATION

—5— LINE OF EQUAL RAINFALL SHOWING
QUANTITY OF 2-YEAR 24-HOUR
RAINFALL, IN INCHES--Interval
0.5 inch

Figure 14.—Precipitation factor, 2-year 24-hour rainfall, in inches
(U.S. Department of Commerce, 1961.

LAGTIME EQUATION FOR SHELBY COUNTY

The following is the regression equation developed by Neely (1984) for computing lagtime of urban basins in Shelby County.

$$LT = 2.05 A^{0.35} P^{-0.87} I^{-0.22}$$

Where

- LT is the computed lagtime, in hours;
- A is the drainage area, in square miles;
- P is average channel condition; and
- I is impervious area, in percent.

The channel condition, P, is defined and computed as follows: The average channel condition between points along the main channel at 100 percent, 75 percent, 50 percent, and 25 percent of the drainage area. If the channel is paved with concrete, use a value of 2; if unpaved, use a value of 1. Estimate the channel condition for partial paving between 1 and 2.

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